

Main properties of new heavy hadrons and the luminosity of hadronic dark matter

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New heavy hadrons and hadronic DM

WIMP Rigid restrictions on $\sigma(WN) \rightarrow$ SIMP

(Wandelt e a, 2000; McGuere e a, 2001; Huo e a, 2016; Luca e a, 2019; Bhattacharya e.a.,2019)

Hadronic DM - one of SI candidate on DM particles $M = (qQ)$

Q is new heavy quark (QCD strong interaction)

Origin of Q :

- a) 4-th generation (Khlopov, Maltony, Novikov, Okun, Vysotsky, Belotsky, Fargion, ...)
- b) Mirror or chiral-symmetric models
- c) Extension of SM with singlet quark

Vector-like interactions of Q with gauge bosons γ and Z . (W).

Strong QCD-type interaction of Q with $q \rightarrow$ coupled states:

$(qQ), (qqQ), (qQQ), (QQQ), \dots$

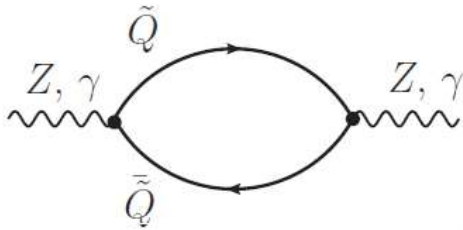
WIMP \rightarrow SIMP: processes $(2 \rightarrow 2) \rightarrow (3 \rightarrow 2)$ (N-changing processes, Bhattacharya e.a.)

Crucial modifications in dynamics of DM evolution (annihilation, scattering, etc.)

EW restrictions on Q

Vector-like interactions of Q with gauge bosons γ and $Z \rightarrow$ cause small contributions into polarizations.

$$L(Q_a, A, Z) = g_a (c_w A_\mu - s_w Z_\mu) \bar{Q}_a \gamma^\mu Q_a, \quad Q_a = Q_s, U, D$$



$P_{\gamma\gamma}, P_{ZZ}, P_{\gamma Z}; (P_{WW} = 0)$ PT parameters

$$S = -U = \frac{ks_w^4}{9\pi} \left[-\frac{1}{3} + 2 \left(1 + 2 \frac{M_{\tilde{Q}}^2}{M_Z^2} \right) \left(1 - \sqrt{\beta} \arctan \frac{1}{\sqrt{\beta}} \right) \right].$$

$$\underline{M_Q > 500 \text{ GeV}} \quad S = |U| < 10^{-2}, T = 0 \quad \beta = 4M_{\tilde{Q}}^2/M_Z^2 - 1$$

PDG 2019: $S, T, U \lesssim 10^{-1}$

No mixing $q \leftrightarrow Q$: FCNC are absent \rightarrow there are no restrictions from rare processes (rare decays, oscillations)

Quantum numbers, isotopic and quark structure of new hadrons

$J^P = 0^-$	$T = \frac{1}{2}$	$M_U = (M_U^0 M_U^-)$	$M_U^0 = \bar{U}u, M_U^- = \bar{U}d$
$J^P = 0^-$	$T = \frac{1}{2}$	$M_D = (M_D^+ M_D^0)$	$M_D^+ = \bar{D}u, M_D^0 = \bar{D}d$
$J = \frac{1}{2}$	$T = 1$	$B_{1U} = (B_{1U}^{++} B_{1U}^+ B_{1U}^0)$	$B_{1U}^{++} = Uuu, B_{1U}^+ = Uud, B_{1U}^0 = Udd$
$J = \frac{1}{2}$	$T = 1$	$B_{1D} = (B_{1D}^+ B_{1D}^0 B_{1D}^-)$	$B_{1D}^+ = Duu, B_{1D}^- = Ddd, B_{1D}^0 = Dud$
$J = \frac{1}{2}$	$T = \frac{1}{2}$	$B_{2U} = (B_{2U}^{++} B_{2U}^+)$	$B_{2U}^{++} = UUU, B_{2U}^+ = UUD$
$J = \frac{1}{2}$	$T = \frac{1}{2}$	$B_{2D} = (B_{2D}^0 B_{2D}^-)$	$B_{2D}^0 = DDu, B_{2D}^- = DDd$
$J = \frac{3}{2}$	$T = 0$	(B_{3U}^{++})	$B_{3U}^{++} = UUU$
$J = \frac{3}{2}$	$T = 0$	(B_{3D}^-)	$B_{3D}^- = DDD$

New heavy meson doublets M_U and M_D

$M_U^0 = (\bar{U}u)$ is stable - candidate on DM particles

Mass of new meson

Mass $M = m(M^0) \approx m(Q)$; $M^0 = (\bar{Q}q)$ (pseudoscalar meson)

$$(\sigma(M)v_r)^{exp} = (\sigma(M)v_r)^{theor}$$

$(\sigma(M)v_r)^{DM} = 2 \cdot 10^{-9} \text{ GeV}^{-2}$ The data on DM relic density

$$(\sigma(M)v_r)^{theor} \approx \sigma(Q\bar{Q} \rightarrow q\bar{q}, gg) = \frac{44\pi}{9} \frac{\alpha_s^2}{M^2}$$

$$M_0 \approx M_Q \approx 10 \text{ TeV}$$

ZE effect

$$(\sigma(M)v_r) = (\sigma(M)v_r)_0 \cdot \frac{2\pi\alpha/v_r}{1 - \exp(-2\pi\alpha/v_r)}$$

At M-scale $\alpha_w \sim 0.03$ and $v \sim 0.1 \rightarrow M \approx 15 \text{ TeV}$.

Fine and hyperfine structure of excited states of heavy hadrons

FINE SPLITTING.

Mass-splitting of $M^0 = (\bar{U}u)$ and $M^- = (\bar{U}d)$

$$\Delta m = m(M^-) - m(M^0)$$

M-mesons $\Delta m > 0$, (~ 1 MeV); (unstable $M^- \rightarrow \underline{\Delta m > m_e}$)

$$\text{Decay: } M^- \rightarrow M^0 e \bar{\nu}_e \quad \Gamma \approx G_F^2 (\Delta m)^5 / 60\pi^3$$

$$\Delta m = (1 - 10) \text{ MeV} \longrightarrow \tau \sim (10^5 - 10^0) \text{ s}$$

M^- is long-lived \rightarrow co-annihilation
 M^- signals in cosmic rays (Bazhutov e.a.)

Hyperfine splitting

Heavy quark symmetry provides relations between masses of the first excited states $\frac{1}{2}(1^-)$ and ground states $\frac{1}{2}(0^-)$ of B and D mesons

$$\begin{aligned} \delta m_K &= 400 \text{ MeV} \\ \delta m_D &= 140 \text{ MeV} \\ \delta m_B &= 45 \text{ MeV} \end{aligned} \quad \frac{m(B^*) - m(B)}{m(D^*) - m(D)} = \frac{m_c}{m_b} \longrightarrow 0.32 \approx 0.31.$$

Then, for the case of heavy meson, $M = 10 \text{ TeV}$, we get:

$$\frac{\delta m(M)}{\delta m(B)} = \frac{m(M^*) - m(M)}{m(B^*) - m(B)} = \frac{m_b}{M} \longrightarrow \delta m(M) \approx 2 \text{ KeV}.$$

The effect of hyperfine splitting has two principal phenomenological consequences in a study of hidden matter:

1. It provides additional channels of interaction of DM with photons and other SM particles.
2. This effect can manifest itself as key-signals in underground detectors (XENON1 etc).

Luminosity of hidden matter

KeV range \rightarrow γ -ray with $\lambda \sim 10^{-9}$ cm.

If $M^0 = (u\bar{U})$ has characteristic size an order of nucleon radius, $R_M \sim 10^{-13}$ cm, then $\lambda \gg R_M$, cross-section is small.

At $\lambda_{trans} \lesssim R_M$, that is $E_\gamma \gtrsim 10$ MeV, the interaction γM^0 can be noticeable. and hidden matter is not dark (luminous hidden matter).

Effect of luminosity can be observed for the case of narrow spectral line, $\Gamma = 1/\tau$ (long-lived excited states).

HFS provides effects with $O(keV)$ electron recoil in direct detection experiments (XENON1T signals, luminous dark matter)

$U(NM) > 0$ and $\sigma(NM \rightarrow NM) \sim 1$ barn, $\lambda = 1/(n\sigma) \sim$ cm.

Repulsive potential of NM interaction and large elastic cross-section lead to absorption and thermalization of heavy DM-particles in the planets and stars.

Low-energy interaction of nucleon and dark matter particles

$U(1) \cdot SU(3)$ -gauge scheme of interaction of nucleons and vector mesons

$$L_{NV} = g_\omega \omega_\mu (\bar{p} \gamma^\mu p + \bar{n} \gamma^\mu n) + \frac{1}{2} g \rho_\mu^0 (\bar{p} \gamma^\mu p - \bar{n} \gamma^\mu n) \\ + \frac{1}{\sqrt{2}} g \rho_\mu^+ \bar{p} \gamma^\mu n + \frac{1}{\sqrt{2}} g \rho_\mu^- \bar{n} \gamma^\mu p,$$

To apply gauge scheme for M -mesons we extend doublet (M^0, M^-) to triplet $M = (M^0, M^-, M_s^-)$, where $M_s^- = (s\bar{U})$.

Lagrangian of low-energy interactions of M -particles with vector singlet V_μ^0 and octet V_μ is defined by the standard gauge form:

$$L_{MV} = (D^\mu M)^\dagger D_\mu M, \quad D_\mu M = (\partial_\mu - itV_\mu^0 - \frac{ig}{\sqrt{3}} V_\mu) M,$$

Physical Lagrangian of interaction of M -particles with vector mesons:

$$L_{MV} = ig_\omega M \omega^\mu (\bar{M}^0 M_{,\mu}^0 - \bar{M}_{,\mu}^0 M^0 + M_{,\mu}^+ M^- - M^+ M_{,\mu}^-) \\ + (ig_\omega M_s \omega_\mu + ig_\phi M_s \phi_\mu) (M_s^+ M_s^{-,\mu} - M_s^{+,\mu} M_s^-) \\ + (\frac{ig}{2} \rho_\mu^0 + ig_\phi M \phi_\mu) (\bar{M}^0 M_{,\mu}^0 - \bar{M}_{,\mu}^0 M^0 + M_{,\mu}^+ M^- - M^+ M_{,\mu}^-) \\ + \frac{ig}{\sqrt{2}} \rho^{+\mu} (\bar{M}^0 M_{,\mu}^- - \bar{M}_{,\mu}^0 M^-) + \frac{ig}{\sqrt{2}} \rho^{-\mu} (M^+ M_{,\mu}^0 - M_{,\mu}^+ M^0).$$

One-meson exchange approach to NM-interaction

Cold DM: Low-energy MNI model $MN \rightarrow (v, s) \rightarrow MN, (\omega, \rho)$

Potential of MN-interaction in Born approximation

$$V(\vec{r}) = -\frac{1}{4\pi^2\mu} \int f(q) \exp(i\vec{q}\vec{r}) d^3q, \quad f(q) \rightarrow \begin{array}{ccc} \text{M} & \text{-----} & \text{M} \\ & \text{v} \quad | \quad \text{s} & \\ \text{N} & \text{-----} & \text{N} \end{array}$$

Asymptote of MN-potential: $V_v(r) = (K_v/r) \exp(-r/r_v)$

$V > 0$ MN-repulsion (at long distance)

Coupled states (MN) at low energy (cold DM) are absent

C.-C. restrictions. The problems of anomalous H and He

Cross-section of low-energy NM interactions

The expression for elastic MN scattering cross-section:

$$\sigma(N_a M_b \rightarrow N_a M_b) = \frac{g^+ m_p^2}{16\pi m_v^4} \left(1 + \frac{k_{ab}}{\sin^2 \theta}\right)^2,$$

where $N_a = (p, n)$, $M_b = (M^0, M^-)$, $g^2/4\pi \approx 3.4$, $\sin \theta = 1/\sqrt{3}$ and $k_{ab} = \pm 1$ for the case of p or n . Here, we used approximate relations $m_p \approx m_n$, $m(M^0) \approx m(M^-)$ and $m_v = m_\rho \approx m_\omega$.

As a result, we get large value of cross-section, for example $\sigma(pM^0 \rightarrow pM^0) \approx 0.9$ barn.

The expressions for non-elastic scattering of type $N_a M_b \rightarrow N_c M_d$, where $N_a = (p, n)$ and $M_b = (M^0, M^-)$

$$\sigma(N_a M_b \rightarrow N_c M_d) = \frac{g^4 m_N^2}{8\pi m_v^4} \left[1 - \frac{\Delta_{ab}}{E_p}\right]^{1/2}$$

Here, $E_p \approx m_p v_r^2/2$ and $\Delta_{ab} = m(M^-) - m(M^0) \pm (m_n - m_p)$ for $p \rightarrow n$ ($n \rightarrow p$)

Consider the reaction $pM^0 \rightarrow nM^+$ From the threshold kinetic energy $E_p^{thr} = \Delta M + \Delta m \equiv \Delta_{11}$ it follows the value of velocity at the threshold $v_r^{thr} = \sqrt{2\Delta_{11}/m_p}$. For the case $\Delta_{11} = 10$ MeV we get rather large relative velocity $v_r^{thr} = 0.1 \gg v_r \sim 10^{-3}$. The reaction $nM^0 \rightarrow pM^-$ can be threshold and non-threshold depending on the value $\Delta M/\Delta m$. We should note that this reaction lead to the final states with unstable particles, they go through two stage, $nM^0 \rightarrow pM^- \rightarrow pM^0 e^- \bar{\nu}_e$.

Interaction of hadronic DM with standard leptons

Charge transition $M^0 \rightarrow M^- W$ is described by effective vertex in the form:

$$L^{eff}(WMM) = iG_{WM} W^{+\mu} (\bar{M}^0 \partial_\mu M^- - \partial_\mu \bar{M}^0 M^-) + h.c.$$

The value of effective constant G_{WM} is determined by matching the expressions for width of decay $M^- \rightarrow M^0 W^- \rightarrow M^0 e^- \bar{\nu}_e$ with help of standard form-factor method and using the model Lagrangian:

$$\Gamma(M^- \rightarrow M^0 e^- \bar{\nu}_e) \approx \frac{g^2 G_{WM}^2 (\Delta M)^5}{15 \cdot 2^4 \pi^3 M_W^4}.$$

The comparison of this expression with standard one leads to the relation

$$G_{WM}^2 = \bar{g}^2 |U_{ud}|^2 / 2^3 \text{ or } G_{WM} = g U_{ud} / 2\sqrt{2}$$

Low-energy interaction of M-particles with Z-boson can be represented in the same form:

$$L^{eff}(ZMM) = iG_{ZM} (\bar{M}_q \partial_\mu M_q - \partial_\mu \bar{M}_q M_q)$$

In contrast to charge vertex, effective coupling G_{ZM} is generated by interactions of Z with both quarks Q and q . So, it is defined by the coupling $g_1 \sin \theta_w$ in vertex ZUU and $g_2 c_q / 4 \cos \theta_w$ in standard vertex Zqq , which are different.

Cross-sections of DM-Lepton scattering

$$\sigma(l^- M^0 \rightarrow \nu_l M^-) = \frac{3g^4 |U_{ud}|^2}{2^{10} \pi M_W^4} s \left(1 - \frac{M^2}{s}\right)^2$$

$l = e, \mu, \tau$ \sqrt{s} is full energy in the center of mass system

Full process $l M^0 \rightarrow \nu_l M^- \rightarrow \nu_l M^0 e \bar{\nu}_e$

Convolution formula for the process $l M^0 \rightarrow \nu_l M^0 e \bar{\nu}_e$:

$$\sigma(l M^0 \rightarrow \nu_l M^0 e \bar{\nu}_e) = \int_a^b dq^2 \sigma(l M^0 \rightarrow \nu_l M^-(q^2)) \frac{q \Gamma(M^-(q^2))}{\pi |q^2 - M_0^2 + i q \Gamma(M^-(q^2))|^2}$$

At $q^2 = M_-^2$ the cross-section has acute peak and the process pass through at small momenta transfer from lepton.

Conclusions

- HDM is not excluded by EW and CC restrictions.
- Large mass of DM hadrons (10 TeV and upper).
- Signals of charge M-decay: metastable charge particle and low-energy leptons.
- Hyperfine mass-splitting in M - M^* : signals - low-energy photons (KeV) and luminosity of DM.
- Analysis of HDM scenario with account of M^* , co-annihilation, absorption and thermalization.
- Description of DM interaction with usual matter.