

Formation of conserved charges at the de Sitter space

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23rd International workshop “What comes beyond the standard models?”
July 10, 2020



- 1 Conserved charges and numbers in Kaluza-Klein-like theories

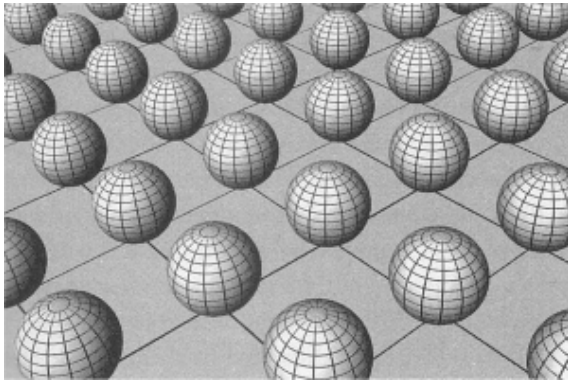
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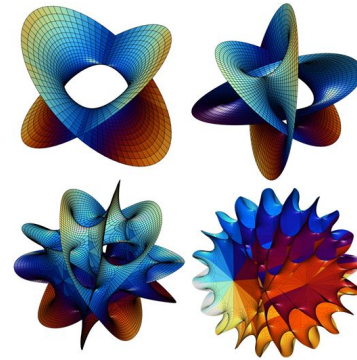
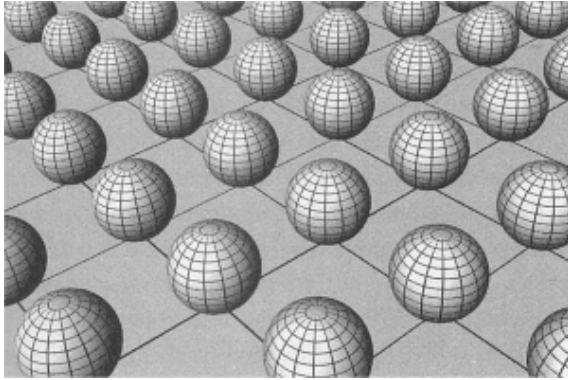
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- 6 Conclusion



Conserved charges and numbers in Kaluza-Klein-like theories

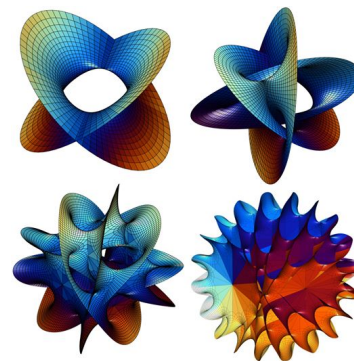
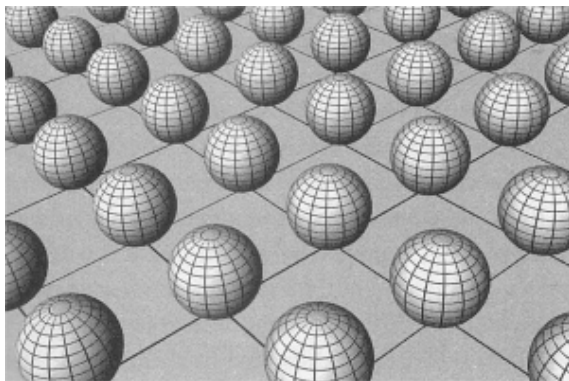


Spatial isometries of extra space

$$ds^2 = g_{ab}(x) dx^a dx^b + k_{mn}(y) dy^m dy^n ; \quad (1)$$

$$\Gamma^a_{bc} \Gamma^b_{da} = 0 ; \quad (2)$$

Conserved charges and numbers in Kaluza-Klein-like theories



Spatial isometries of extra space

$$ds^2 = g_{ab}(x) dx^a dx^b + k_{mn}(y) dy^m dy^n ; \quad (1)$$

$$r_{ab} = r_{ba} = 0 : \quad (2)$$

Noether's current and charge (number)

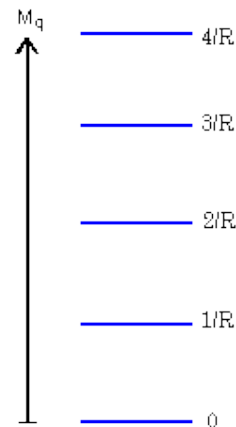
$$J^a = \frac{\partial L_m(\dots)}{\partial (\partial_a \dots)} \delta^a_b \dots \quad (3)$$

$$Q = \int J^0 d^3x = \text{const} : \quad (4)$$

Transition to effective 4-dim theory

$$(x; y) = \sum_{q=0}^{\infty} \int d^4x d^d y \frac{1}{|g|} \frac{1}{|k|} \frac{1}{2} \eta_{AB} \eta^{AB} = \int d^4x d^d y \frac{1}{|g|} \sum_{q=0}^{\infty} \frac{1}{2} (\eta_{AB})^2 (M_q^2 + \dots) \frac{2}{q} ; \quad (5)$$

$$S = \int d^4x d^d y \frac{1}{|g|} \sum_{q=0}^{\infty} \frac{1}{2} (\eta_{AB})^2 (M_q^2 + \dots) \frac{2}{q} ; \quad (6)$$



Conserved charges and numbers in Kaluza-Klein-like theories

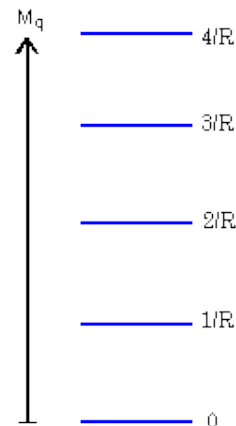
Transition to effective 4-dim theory

$$(x; y) = \sum_{q=0}^{\infty} \int d^4x d^d y \rho_{|j|} \rho_{|k|} \frac{1}{2} \eta_{AB} \eta^{AB} \frac{1}{2} = \quad (5)$$

$$M_q \frac{dY_q(y)}{dy} = M_q^2 Y_q(y); \quad q=R; \quad q \geq N:$$

$$S = \int d^4x d^d y \rho_{|j|} \rho_{|k|} \frac{1}{2} \eta_{AB} \eta^{AB} \frac{1}{2} = \quad (6)$$

$$= \int d^4x \rho_{|j|} \sum_{q=0}^{\infty} \frac{1}{2} (\eta_{AB} \eta^{AB})^2 (M_q^2 + \eta_{AB} \eta^{AB}) \frac{1}{2} :$$

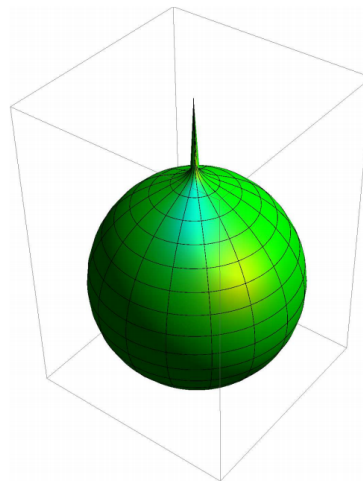
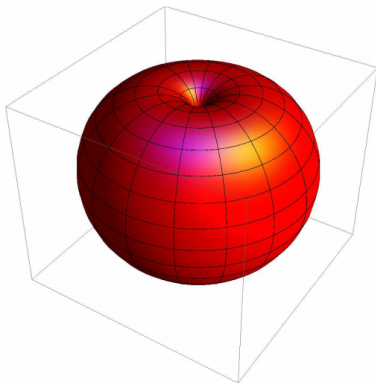


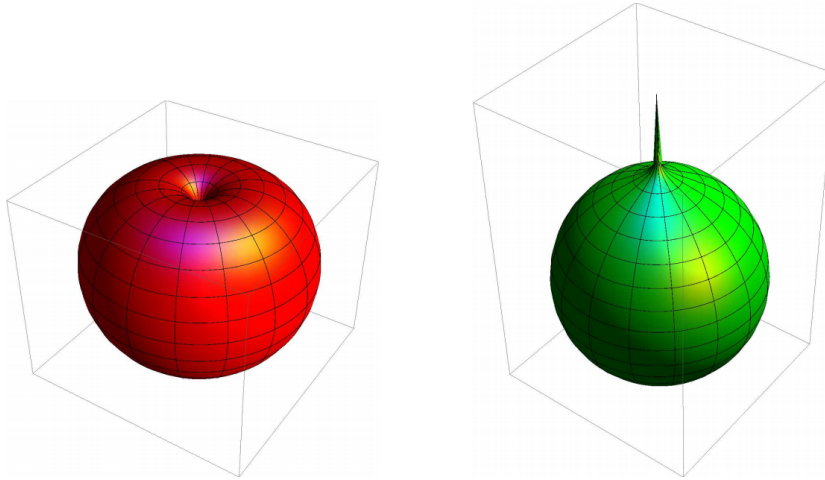
Effective 4-dim Noether's current and charge (number)

$$j = \frac{\delta L_4}{\delta (\delta \eta^n)} (\eta^n)_m ; \quad (\eta^n)_m = \int d^4x d^d y \rho_{|j|} \rho_{|k|} \eta^n \eta_m \quad (7)$$

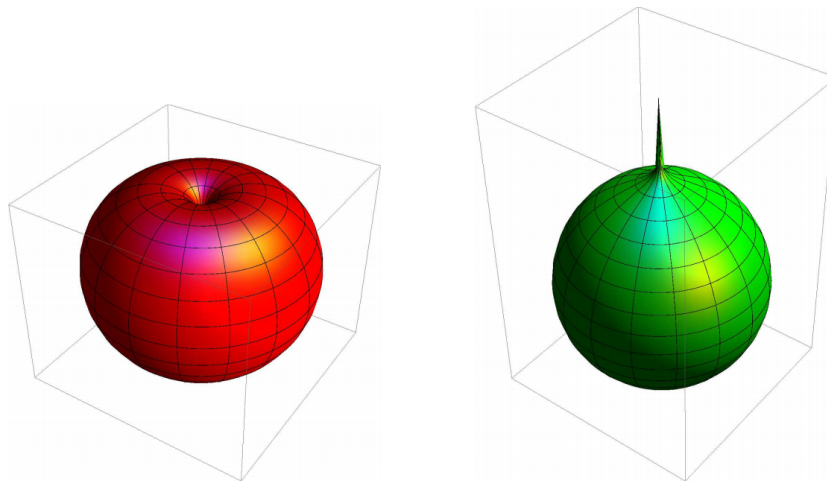
$$Q = \int d^3x j^0 \rho_{|j|} = \text{const} : \quad (8)$$

Apple-like extra space models with $U(1)$ -symmetry



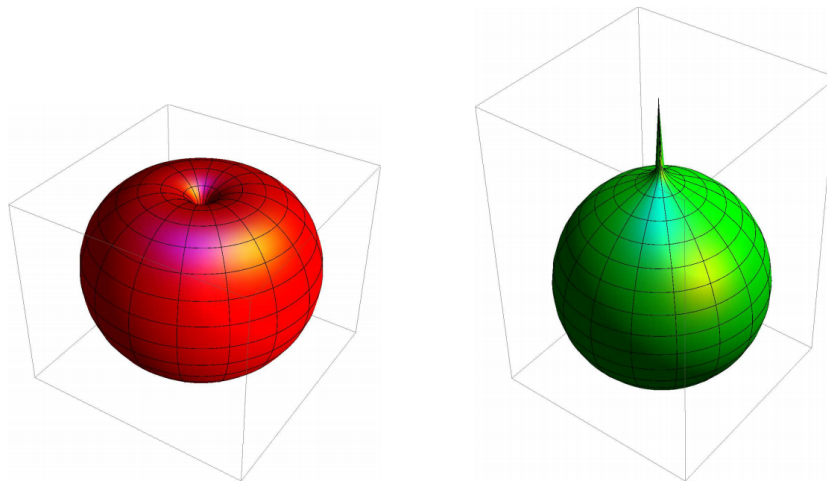


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- Compact 2-dim apple-like manifold have $U(1)$ -symmetry associated with polar rotational isometry.
- Unlike the one-dimensional compact extra space, a 2-dim manifold has a non-zero Ricci scalar and can be perturbed.
- Considered in the framework of warped extra dimensions. It is developed in different works: [arxiv:0706.0676](https://arxiv.org/abs/0706.0676), [arxiv:1511.01869](https://arxiv.org/abs/1511.01869), [arxiv:hep-th/0302067](https://arxiv.org/abs/hep-th/0302067), etc.

Space-time setting

$$S = \frac{m_D^{D-2}}{2} \int d^D X^\rho \sqrt{|G|} [f(R) + L_m]; \quad f(R) = aR^2 + R + c; \quad (9)$$

$$ds^2 = G_{MN} dX^M dX^N = g_{\mu\nu}(x) dx^\mu dx^\nu + k_{mn}(x; y) dy^m dy^n; \quad (10)$$

$$g_{\mu\nu} = \text{diag}(1; e^{2Ht}; e^{2Ht}; e^{2Ht}); \quad (11)$$

$$k_{mn}(x; y) = k_{mn}^{\text{st}}(y) \quad (12)$$

Apple-like extra space models with U(1)-symmetry

Space-time setting

$$S = \frac{m_D^D}{2} \int d^D X^P \sqrt{|G|} [f(R) + L_m]; \quad f(R) = aR^2 + R + c; \quad (9)$$

$$ds^2 = G_{MN} dX^M dX^N = g_{\mu\nu}(x) dx^\mu dx^\nu + k_{mn}(x; y) dy^m dy^n; \quad (10)$$

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$$k_{mn}(x; y) = \delta_{mn} + k_{mn}^{\text{st}}(y) \quad (12)$$

Extra space configuration

$$k_{mn}(x; y) = r(\rho; t)^2 (d^2 + \sin^2 \rho) \delta_{mn} + k_{mn}^{\text{st}}(y) \quad (13)$$

$$k_{mn}^{\text{st}}(y) = r_0(\rho)^2 (d^2 + \sin^2 \rho) \delta_{mn}; \quad (14)$$

$$r(\rho; t) = r_0(\rho) e^{H(\rho; t)} = r_0 e^{H(\rho) + H(\rho; t)} \quad (15)$$

Inflationary extra space relaxation in the presence of (scalar) field

Matter content

$$L_m = \frac{1}{2} G^{MN} \partial_M \phi \partial_N \phi - V(\phi); \quad V(\phi) = \frac{1}{2} m^2 \phi^2; \quad (16)$$

$$T_{MN} = -2 \frac{\partial L_m}{\partial G^{MN}} + G_{MN} L_m; \quad (17)$$

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Dinamical equations

$$R_{MN} f^0 = \frac{1}{2} f(R) k_{MN}^{st} + r_M r_N f^0 - k_{MN}^{st} f^0 = \frac{1}{m_D^2} T_{MN}; \quad (18)$$

$$d = V^0(\phi); \quad (19)$$

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$$d = -V^0(\phi); \quad (19)$$

- To reduce the order of the PDEs system, we take the standard equation for the connection of Ricci scalar with the metric as the third equation. We also compute the trace of Einstein's equations to simplify. As a result we obtain a second order system of 3 equations for 3 unknown functions: $(t; \phi; \psi)$, $R(t; \phi; \psi)$, $(t; \phi; \psi)$.

Inflationary extra space relaxation in the presence of (scalar) field

Stationary symmetrical equations for metric $k_{mn}^{st}(y)$: $g_{st}(\cdot)$, $R_{st}(\cdot)$, $\Lambda_{st}(\cdot)$

$$e^2 r^2 \left[3aR^2 + c + R - 6H^2(2aR+1) - 3m^2 r^2 + 4(2aR+1) \cot \theta + \right. \\ \left. + 4(2aR+1) \left[8a \cot \theta (R + R) + 4(2aR+1) + \right]^2 = 0; \quad (20)$$

$$e^2 r^2 \left[12H^2 R - 2 \cot \theta + 1 \right] = 0; \quad (21)$$

$$e^2 m^2 r^2 \cot \theta + = 0; \quad (22)$$

Inflationary extra space relaxation in the presence of (scalar) field

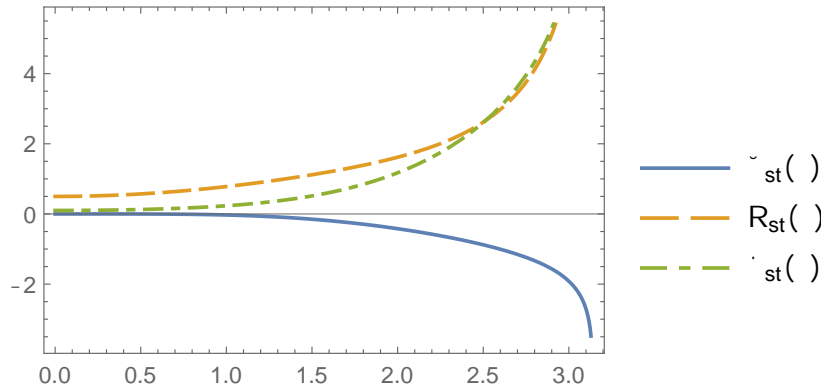
Stationary symmetrical equations for metric $k_{mn}^{st}(y)$: $\tilde{r}_{st}(\cdot)$, $R_{st}(\cdot)$, $\dot{r}_{st}(\cdot)$

$$e^2 r^2 \left[3 a R^2 + c + R \right] - 6 H^2 \left[2 a R + 1 \right] - 3 m^2 r^2 + 4 \left[2 a R + 1 \right] \cot +$$

$$+ 4 \left[2 a R + 1 \right] \left[8 a \cot R + R \right] + 4 \left[2 a R + 1 \right] + \dots^2 = 0; \quad (20)$$

$$e^2 r^2 \left[12 H^2 R \right] - 2 \cot + \dots = 0; \quad (21)$$

$$e^2 m^2 r^2 \cot + \dots = 0; \quad (22)$$



Small perturbations approximation

$$\begin{aligned} (t; \delta) &= \text{st}(\delta) + (t; \delta); & (t; \delta) &= \text{st}(\delta); \\ R(t; \delta) &= R_{\text{st}}(\delta) + R(t; \delta); & R(t; \delta) &= R_{\text{st}}(\delta); \\ (t; \delta) &= \text{st}(\delta) + (t; \delta); & (t; \delta) &= \text{st}(\delta); \end{aligned} \tag{23}$$

Inflationary extra space relaxation in the presence of (scalar) field

Small perturbations approximation

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 (t; ;) &= {}_{st}(\) + (t; ;); & (t; ;) & {}_{st}(\);
 \end{aligned} \tag{23}$$

Linearized equations

$$\begin{aligned}
 e^2 r^2 3 R 4aH^2 2aR 1 + 8a R \csc^2 8a R \cot + 1 + \\
 + 2 3 m^2 3 R 4aH^2 + aR + 1 + c 2H^2 m^2 2 12aHR t + \\
 + 4 2aR + 1 tt + 18aH R_t 4a R_{tt} + 6H t + 8a R \cot 4
 \end{aligned} \tag{24}$$

$$4 2aR + 1 \csc^2 4 2aR + 1 \cot + 8a R R + 2 = 0;$$

$$e^2 r^2 24H^2 2R + 4 3H t + tt R 2 \cot + \csc^2 + = 0; \tag{25}$$

$$e^2 r^2 m^2 2 + + 3H t + tt \cot \csc^2 = 0: \tag{26}$$

In stationary extra space relaxation in the presence of (scalar) field

Initial conditions (for example random traveling wave in $n=2$ mode)

$$\begin{aligned} \psi(t; \mathbf{x}) &= \psi_2(t; \mathbf{x}) \sin(2\mathbf{x}) + \psi_2 \left(t + \frac{n}{2} \right); \cos(2\mathbf{x}); \\ \psi(t; \mathbf{x}) &= \psi_2(t; \mathbf{x}) \sin(2\mathbf{x}) + \psi_2 \left(t + \frac{n}{2} \right); \cos(2\mathbf{x}); \end{aligned} \quad (27)$$

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Accumulation of U(1)-number initial asymmetry

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Effective 4-dim U(1)-number before the relaxation ends

$$\begin{aligned}
 Q(t) &= \int_0^Z \int_0^{2\pi} \int_0^{2\pi} r^2 e^2 \sin \theta d\theta d\phi = \\
 &= \int_0^Z \int_0^{2\pi} \int_0^{2\pi} (t; \theta) (t; \phi) r^2 e^2 \sin \theta d\theta d\phi : \quad (28)
 \end{aligned}$$

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$$\begin{aligned}
 Q(t) &= \int_{\mathcal{D}} \mathcal{Q} \, r^2 e^2 \sin \theta \, d\theta \, d\phi = \\
 &= \int_{\mathcal{D}} \mathcal{Q}(t; \theta, \phi) \, r^2 e^2 \sin \theta \, d\theta \, d\phi : \quad (28)
 \end{aligned}$$

Problem of charge (number) transfer to the lowest KK-mode

The total charge of the KK-tower

$$\begin{aligned}
 Q &= \int J_0^p \frac{1}{|g|} \frac{1}{|k|} d^3x d^d y \\
 &= \sum_{n=0}^{\infty} \int \chi_n \frac{1}{|g|} \frac{1}{|k|} d^3x = \quad (29) \\
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 &= \sum_{n=1}^{\infty} \int \chi_n \frac{1}{|g|} \frac{1}{|k|} d^3x :
 \end{aligned} \tag{29}$$

- The lower level of the KK-tower does not contribute to the total charge. The charge of its particles is zero - therefore, the massive KK-modes cannot decay into known particles (which should be located at the lower level of the KK-towers).

Fermion splitting in extra space with angle profuse

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Angle profuse extra space

$$ds^2 = g(x) dx dx + r_0^2 d^2 + b^2 \sin^2 d' d'^2 ; \quad (30)$$

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Higher-dimensional fermionic action

$$S = \int d^6 x \sqrt{|g|} \bar{\psi} \gamma^{\mu} \partial_{\mu} \psi + \int d^6 x \sqrt{|g|} \bar{\psi} \gamma^{\mu} \partial_{\mu} \psi + \int d^6 x \sqrt{|g|} \bar{\psi} \gamma^{\mu} \partial_{\mu} \psi ; \quad (31)$$

where γ^{μ} is at gamma matrices

$$\gamma^0 = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} ; \quad \gamma^1 = \begin{pmatrix} 0 & i \\ i & 0 \end{pmatrix} ; \quad \gamma^2 = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} ; \quad (32)$$

and h^A_B is the frame field:

$$g^{AB} = h^A_{\mu} h^{\mu B} ; \quad (33)$$

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$$S = \int d^6 x \sqrt{|g|} \bar{\psi} \gamma^A \gamma^B h_{AB}^C \psi ; \quad (31)$$

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and h_{AB}^C is the frame field:

$$g^{AB} = h_{AC}^A h_{B}^B : \quad (33)$$

- You can find a detailed derivation of fermion splitting in the paper [arxiv: 0706.0676](https://arxiv.org/abs/0706.0676).

Fermion splitting in extra space with angle profuse

Kaluza-Klein decomposition of lowest level

$$\chi^A = \sum_I Y_I(\cdot; \cdot) \psi_I(x) = \sum_I \frac{e^{iI \cdot}}{\sqrt{2}} \begin{pmatrix} \psi_I(\cdot) \\ \psi_I(x) \end{pmatrix}; \quad (34)$$

where the form of $\psi_I(\cdot)$ and $\psi_I(x)$ are computed from extra metric. Effective fermions ψ_I and ψ_I are indistinguishable for the massless KK-level.

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Massless effective 4-dim modes

$$S = \int d^6 X \int d^4 x \sum_I \bar{\psi}_I \gamma^{\mu\nu} \psi_I h_{AB}^{\mu\nu} \psi_I \psi_I; \quad I = d, b=2e, \dots; 0, \dots; +bb=2c: \quad (35)$$

Limitation of mode number comes from the normalization condition:

$$\int d^6 X \int d^4 x \bar{\psi}_I \psi_I = \int d^4 x \int d^2 x \bar{\psi}_I \psi_I + \dots; \quad (36)$$

Correspondence of currents

$$\begin{aligned}
 J^m &= \frac{\partial L}{\partial (\partial_m \Psi)} \partial^m \Psi = i \bar{\Psi} h_{\tilde{A}}^m \Gamma^{\tilde{A}} \partial^m \Psi \quad (=) \\
 j &= \frac{\partial L_4}{\partial (\partial_\mu \psi)} \partial^\mu \psi = i \int_{\tilde{I}} \bar{\psi} \Gamma^{\tilde{I}} \partial^\mu \psi; \quad t_{\mu\nu} = \int_{\tilde{I}} Y_{\tilde{I}} \partial_\mu \psi \partial_\nu \bar{\psi} d^2 y = i t_{\mu\nu}; \quad (37)
 \end{aligned}$$

Fermion splitting in extra space with angle profuse

Correspondence of currents

$$\begin{aligned}
 j^m &= \frac{\partial L}{\partial (\partial_m \Psi)} \partial^m \Psi = i \bar{\Psi} h_{\tilde{A}}^m \Gamma^{\tilde{A}} \partial^m \Psi \Rightarrow \\
 j^{\mu\nu} &= \frac{\partial L_4}{\partial (\partial_\mu \Psi)} \partial^\nu \Psi - \frac{\partial L_4}{\partial (\partial_\nu \Psi)} \partial^\mu \Psi = i \int_{\mathcal{V}} \bar{\Psi} \Gamma^{\mu\nu} \Psi d^3x = i \int_{\mathcal{V}} \bar{\Psi} \Gamma^{\mu\nu} \Psi d^3x = i \int_{\mathcal{V}} \bar{\Psi} \Gamma^{\mu\nu} \Psi d^3x; \quad (37)
 \end{aligned}$$

U(1)-number

Take the angle profuse parameter $b = 4$ for example.

Then we have triplet splitting: $l = 1; 0; +1$.

$$\begin{aligned}
 Q &= \int_{\mathcal{V}} j^0 d^3x = \int_{\mathcal{V}} j^0 d^3x = \\
 &= i \int_{\mathcal{V}} (\psi_{+1}^\dagger \psi_{+1} - \psi_{-1}^\dagger \psi_{-1}) d^3x = N_{+1} - N_{-1} = \text{const}; \quad (38)
 \end{aligned}$$

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- The accumulated charges (numbers) are then conserved because of the symmetry of effective 4-dimensional theory. However, in the usual case, the charge is realized by massive KK-modes, which are not capable of decaying into known ones due to the symmetry. Such a mechanism is suitable for generating stable dark matter, but is not suitable for explaining the baryon number.

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- It is possible to avoid this limitation in a model where the main KK-level of multidimensional fermions splits into a multiplet. Therefore, it acquires an internal moment - that is, the ability to carry an effective 4-dim charge (number). This splitting becomes possible in extra spaces with an angle profuse.

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- It is possible to avoid this limitation in a model where the main KK-level of multidimensional fermions splits into a multiplet. Therefore, it acquires an internal moment - that is, the ability to carry an effective 4-dim charge (number). This splitting becomes possible in extra spaces with an angle profuse.

- The dynamics of extra space in the early Universe leads to its stabilization and symmetrization, but at the same time causes the symmetry of its final asymptotically stable state to be “initially broken”.
- Violation of the extra space symmetry at the inflationary stage leads to the establishment of non-zero initial values of symmetry-associated charges (numbers) after the inflation.
- The accumulated charges (numbers) are then conserved because of the symmetry of effective 4-dimensional theory. However, in the usual case, the charge is realized by massive KK-modes, which are not capable of decaying into known ones due to the symmetry. Such a mechanism is suitable for generating stable dark matter, but is not suitable for explaining the baryon number.
- It is possible to avoid this limitation in a model where the main KK-level of multidimensional fermions splits into a multiplet. Therefore, it acquires an internal moment - that is, the ability to carry an effective 4-dim charge (number). This splitting becomes possible in extra spaces with an angle profuse.

[arxiv: 2006.01329](https://arxiv.org/abs/2006.01329)

[doi: 10.3390/particles3020027](https://doi.org/10.3390/particles3020027)

Thanks for you attention!

Any questions?