Formation of conserved charges at the de Sitter space

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■ Conserved charges and nubmers in Kaluza-Klein-like theories

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- 2 Apple-like extra space models with U(1)-symmetry

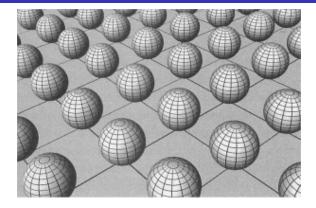
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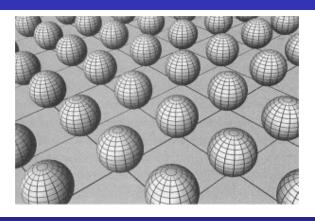
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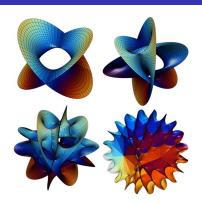
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- 6 Conclusion





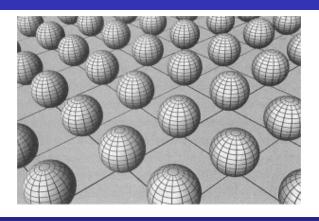


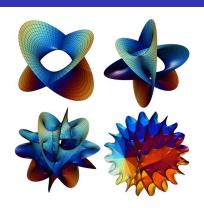


Spatial isometries of extra space

$$ds^{2} = g_{\mu\nu}(x)dx^{\mu}dx^{\nu} + k_{mn}(y)dy^{m}dy^{n}, \qquad (1)$$

$$\nabla_a \, \xi_b - \nabla_b \, \xi_a = 0 \,. \tag{2}$$





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Neother's current and charge (number)

$$J^{a} = \frac{\partial L_{\mathrm{m}}(\chi)}{\partial (\partial_{a}\chi)} \xi^{b} \partial_{b}\chi - \xi^{a} L_{\mathrm{m}}(\chi), \qquad (3)$$

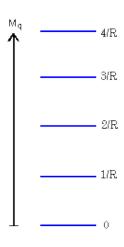
$$Q = \int J^0 \sqrt{|g|} \sqrt{|k|} \, d^3 x \, d^d y = \text{const}.$$
 (4)

Transition to effective 4-dim theory

$$\chi(x,y) = \sum_{q=0}^{\infty} \chi_q(x) Y_q(y) , \quad \left\{ \begin{array}{l} \Box_d Y_q(y) = M_q^2 Y_q(y) ,\\ M_q \approx q/R , \quad q \in \mathbb{N} . \end{array} \right.$$
 (5)

$$S \simeq \int d^4x d^dy \sqrt{|g|} \sqrt{|k|} \frac{1}{2} \left[\partial_A \chi \partial^A \chi - \mu^2 \chi^2 \right] =$$

$$= \int d^4x \sqrt{|g|} \sum_{q=0}^{\infty} \frac{1}{2} \left[(\partial \chi_q)^2 - (M_q^2 + \mu^2) \chi_q^2 \right].$$
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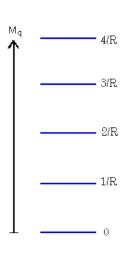


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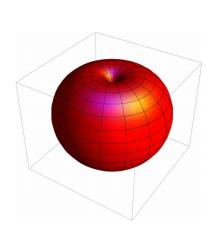
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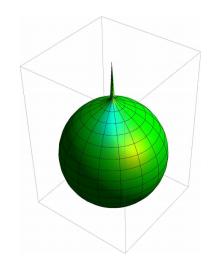


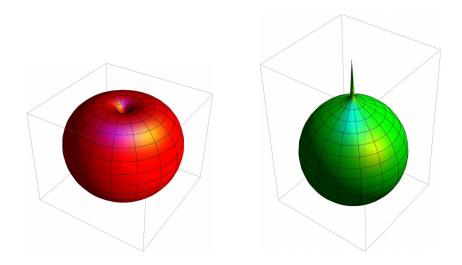
Effective 4-dim Neother's current and charge (number)

$$j^{\alpha} = \frac{\partial \mathcal{L}_4}{\partial (\partial_{\alpha} \phi^n)} (t)_m^n \phi^m , \qquad (t_i)_m^n = \int Y_n \xi^a \partial_a Y_m \sqrt{|k|} \, d^d y$$
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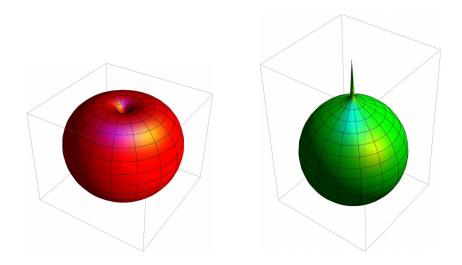
$$Q = \int j^0 \sqrt{|g|} \, d^3 x = \text{const.} \tag{8}$$



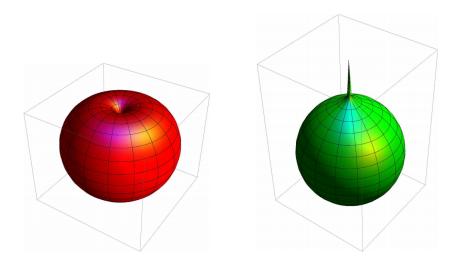




■ Compact 2-dim apple-like manifold have U(1)-symmetry associated with polar rotational isometry.



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- Unlike the one-dimensional compact extra space, a 2-dim manifold has a non-zero Ricci scalar and can be perturbed.
- Considered in the framework of warped extra dimensions. It is developed in different works: arxiv:0706.0676, arxiv:1511.01869, arxiv:hep-th/0302067, etc.

Space-time setting

$$S = \frac{m_D^{D-2}}{2} \int d^D X \sqrt{|G|} \left[f(R) + L_{\rm m} \right], \quad f(R) = aR^2 + R + c. \tag{9}$$

$$ds^{2} = G_{MN}dX^{M}dX^{N} = g_{\mu\nu}(x)dx^{\mu}dx^{\nu} + k_{mn}(x,y)dy^{m}dy^{n}, \qquad (10)$$

$$g_{\mu\nu} = diag(1, -e^{2Ht}, -e^{2Ht}, -e^{2Ht}),$$
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$$k_{mn}(x,y) \xrightarrow{t \to \infty} k_{mn}^{\text{st}}(y)$$
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Extra space configuration

$$k_{mn}(x,y) = r(\theta,\phi,t)^2 (d\theta^2 + \sin\theta \, d\phi^2) \xrightarrow{t \to \infty}$$
 (13)

$$\xrightarrow{t \to \infty} k_{mn}^{\text{st}}(y) = r_0(\theta)^2 (d\theta^2 + \sin\theta \, d\phi^2), \qquad (14)$$

$$r(\theta, \phi, t) = r_0(\theta) e^{\delta \beta(\theta, \phi, t)} = r_0 e^{\beta(\theta) + \delta \beta(\theta, \phi, t)}$$
(15)

Matter content

$$L_{\rm m} = \frac{1}{2} G^{MN} \partial_M \chi \partial_N \chi - V(\chi), \quad V(\chi) = \frac{1}{2} m^2 \chi^2.$$
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$$T_{MN} = -2\frac{\partial L_{\rm m}}{\partial G^{MN}} + G_{MN}L_{\rm m}. \tag{17}$$

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Dinamical equations

$$R_{MN}f' - \frac{1}{2}f(R)k_{MN}^{\text{st}} + \nabla_M \nabla_N f' - k_{MN}^{\text{st}} \Box f' = \frac{1}{m_D^{D-2}} T_{MN}.$$
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$$\Box_d \chi = -V'(\chi) \,, \tag{19}$$

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■ To reduce the order of the PDEs system, we take the standard equation for the connection of Ricci scalar with the metric as the third equation. We also compute the trace of Einstein's equations to simplify. As a result we obtain a second order system of 3 equations for 3 unknown functions: $\beta(t, \theta, \phi)$, $R(t, \theta, \phi)$, $\chi(t, \theta, \phi)$.

Stationary symmetrical equations for metric $k_{mn}^{\text{st}}(y)$: $\beta_{\text{st}}(\theta)$, $R_{\text{st}}(\theta)$, $\chi_{\text{st}}(\theta)$

$$e^{2\beta}r^{2}\left(3(aR^{2}+c+R)-6H^{2}(2aR+1)-3\kappa m^{2}\chi^{2}\right)+4(2aR+1)\beta_{\theta}\cot\theta+ +4(2aR+1)\beta_{\theta\theta}-8a(\cot\theta R_{\theta}+R_{\theta\theta})+4(2aR+1)+\kappa\chi_{\theta}^{2}=0,$$
 (20)

$$e^{2\beta}r^2(12H^2 - R) - 2(\beta_\theta \cot \theta + \beta_{\theta\theta} - 1) = 0,$$
 (21)

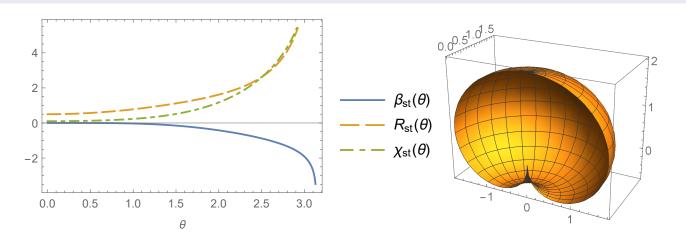
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Small pertribations approximation

$$\beta(t,\theta,\phi) = \beta_{\rm st}(\theta) + \delta\beta(t,\theta,\phi), \quad \delta\beta(t,\theta,\phi) \ll \beta_{\rm st}(\theta),$$

$$R(t,\theta,\phi) = R_{\rm st}(\theta) + \delta R(t,\theta,\phi), \quad \delta R(t,\theta,\phi) \ll R_{\rm st}(\theta),$$

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Linearized equations

$$e^{2\beta}r^{2}\left(3\delta R(4aH^{2}-2aR-1)+8a\delta R_{\phi\phi}\csc^{2}\theta-8a\delta R(\beta_{\theta}\cot\theta+\beta_{\theta\theta}-1)+\right.$$

$$+2\left(3\delta\chi\kappa m^{2}\chi-3\delta\beta\left(R(-4aH^{2}+aR+1)+c-2H^{2}-\kappa m^{2}\chi^{2}\right)-12aHR\delta\beta_{t}+\right.$$

$$+4\left(2aR+1\right)\delta\beta_{tt}+18aH\delta R_{t}-4a\delta R_{tt}+6H\delta\beta_{t}\right)\right)+8a\delta R_{\theta}\cot\theta-4\delta\beta_{\theta\theta}-\tag{24}$$

$$-4\left(2aR+1\right)\delta\beta_{\phi\phi}\csc^{2}\theta-4\left(2aR+1\right)\delta\beta_{\theta}\cot\theta+8a\left(\delta R_{\theta\theta}-R\delta\beta_{\theta\theta}\right)+2\kappa\delta\chi_{\theta}\chi_{\theta}=0,$$

$$e^{2\beta}r^{2}\left(\delta\beta(24H^{2}-2R)+4(3H\delta\beta_{t}+\delta\beta_{tt})-\delta R\right)-2\left(\delta\beta_{\theta}\cot\theta+\delta\beta_{\phi\phi}\csc^{2}\theta+\delta\beta_{\theta\theta}\right)=0,\tag{25}$$

$$e^{2\beta}r^{2}\left(m^{2}(2\delta\beta\chi+\delta\chi)+3H\delta\chi_{t}+\delta\chi_{tt}\right)-\delta\chi_{\theta}\cot\theta-\delta\chi_{\phi\phi}\csc^{2}\theta-\delta\chi_{\theta\theta}=0.\tag{26}$$

Initial conditions (for example random traveling wave in n=2 mode)

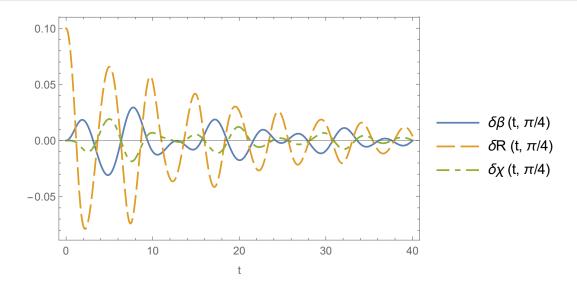
$$\delta\beta(t,\theta,\phi) = \delta\beta_2(t,\theta)\sin(2\phi) + \delta\beta_2\left(t + \frac{n\pi}{2},\theta\right)\cos(2\phi),$$

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Accumulation of U(1)-number initial asymmetry

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Effective 4-dim U(1)-number before the relaxation ends

$$Q(t) = \int \partial^{0} \chi \partial_{\phi} \chi \, r^{2} e^{2\beta} \sin \theta \, d\theta d\phi =$$

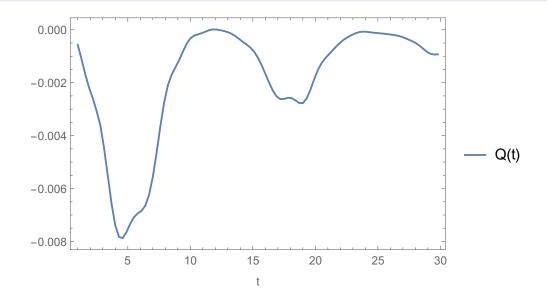
$$= \int \partial^{0} \delta \chi(t, \theta, \phi) \partial_{\phi} \delta \chi(t, \theta, \phi) \, r^{2} e^{2(\beta_{st}(\theta) + \delta\beta(t, \theta, \phi))} \sin \theta \, d\theta d\phi \,. \tag{28}$$

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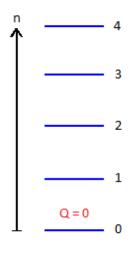
The total charge of the KK-tower

$$Q = \int J^{0} \sqrt{|g|} \sqrt{|k|} d^{3}x d^{d}y \sim$$

$$\sim \int \sum_{n=0}^{\infty} n \chi_{n}^{*} \partial^{0} \chi_{n} \sqrt{|g|} d^{3}x = \qquad (29)$$

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■ The lower level of the KK-tower does not contribute to the total charge. The charge of its particles is zero - therefore, the massive KK-modes cannot decay into known particles (which should be located at the lower level of the KK-towers).

Angle profuse extra space

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Higher-dimentional fermionic action

$$S_{\Psi} = \int d^6 x \sqrt{|G|} \, i \overline{\Psi} h_{\tilde{A}}^B \Gamma^{\tilde{A}} \nabla_B \Psi \,, \tag{31}$$

where $\Gamma^{\tilde{A}}$ is flat gamma matrices

$$\Gamma_{\nu} = \begin{pmatrix} \gamma_{\nu} & 0 \\ 0 & -\gamma_{\nu} \end{pmatrix}, \quad \Gamma_{\theta} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}, \quad \Gamma_{\varphi} = \begin{pmatrix} 0 & i \\ i & 0 \end{pmatrix}, \quad (32)$$

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■ You can find a detailed derivation of fermion splitting in the paper arxiv: 0706.0676.

Kaluza-Klein decomposition of lowest level

$$\Psi\left(x^{A}\right) = \sum_{l} Y_{l}(\theta, \varphi) \Psi_{l}(x) = \sum_{l} \frac{e^{il\varphi}}{\sqrt{2\pi}} \begin{pmatrix} \alpha_{l}(\theta)\psi_{l}(x) \\ \beta_{l}(\theta)\xi_{l}(x) \end{pmatrix}, \tag{34}$$

where the form of $\alpha_l(\theta)$ and $\beta_l(\theta)$ are computed from extra metric. Effective fermions ψ_l and ξ_l are indistinguishable for the massles KK-level.

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Massles effective 4-dim modes

$$S = \int d^{6}X \sqrt{|G|} i \overline{\Psi} h_{\tilde{A}}^{B} \Gamma^{\tilde{A}} \nabla_{B} \Psi \sim$$

$$\sim \int \sqrt{-g} d^{4}x \sum_{l} i \overline{\psi}_{l} \gamma_{\mu} \partial^{\mu} \psi_{l}, \qquad l = -\lceil b/2 \rceil, ..., 0, ..., + \lfloor b/2 \rfloor. \tag{35}$$

Limitation of mode number comes from the normalization condition:

$$\int d^6 X \sqrt{|G|} \,\bar{\Psi}\Psi = \int d^4 x \sqrt{|g|} \,\sum_l \left(\bar{\psi}_l \psi_l + \bar{\xi}_l \xi_l\right) \,. \tag{36}$$

Correspandence of currents

$$J^{m} = \frac{\partial \mathcal{L}}{\partial(\partial_{m}\Psi)} \partial_{\varphi}\Psi = i\overline{\Psi}h_{\tilde{A}}^{m}\Gamma^{\tilde{A}}\partial_{\varphi}\Psi \implies$$

$$j^{\mu} = \frac{\partial \mathcal{L}_{4}}{\partial(\partial_{\mu}\psi_{l})} t_{ll'}\psi_{l'} = i\sum_{l} l\overline{\psi_{l}}\gamma^{\mu}\psi_{l}, \qquad t_{ll'} = \int Y_{l} \partial_{\varphi}Y_{l'}\sqrt{k} d^{2}y = il\delta_{ll'}, \qquad (37)$$

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U(1)-number

Take the angle profuse parameter b = 4 for example.

Then we have triplet splitting: l = -1, 0, +1.

$$Q = \int J^{0} \sqrt{|G|} d^{3}x d^{2}y = \int j^{0} \sqrt{|g|} d^{3}x =$$

$$= \int i(\psi_{+1}^{\dagger} \psi_{+1} - \psi_{-1}^{\dagger} \psi_{-1}) d^{3}x = N_{+1} - N_{-1} = \text{const}.$$
(38)

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- Violation of the extra space symmetry at the inflationary stage leads to the establishment of non-zero initial values of symmetry-associated charges (numbers) after the inflation.

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Thanks for you attention!

Any questions?