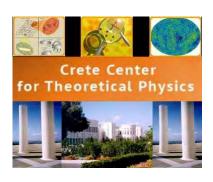
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Emergent gravity and the selftuning of the cosmological constant

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Self-tuning 2.0,

Introduction

- The cosmological constant problem is arguably the most important short-coming today of our understanding of the physical world.
- It signifies the violent clash between gravity and quantum field theory, more so than the black hole information paradox problem.
- In four-dimensional Einstein gravity a non-zero vacuum energy entails irrevocably the acceleration of the univers:

$$G_{\mu\nu} = \frac{1}{2} \Lambda \ g_{\mu\nu}$$

• Fine-tuning the cosmological constant does not solve the problem as we can tune a single constant while the quantum corrections to the vacuum energy are scale dependent.

reviews: Weinberg, Rubakov, Hebecker+Wetterich, Burgess

The higher-dimensional hope

• It was argued by several authors that the existence of higher (than four) dimensions offers the possibility to alleviate the cosmological constant problem.

Rubakov+Shaposhnikov,

- The rough idea is that the SM-induced vacuum energy, instead of curving the 4-d world/brane, could be absorbed by bulk fields.
- For this idea to be effective, the mechanism must be quasi-generic: "any" cosmological constant must "relax", absorbed by the bulk dynamics.
- Any such mechanism must be intertwined tightly with cosmology as we have good reasons to believe that a large cosmological constant played an important role in the early universe, with observable consequences today.

 $D.\ Kazanas,\ Englert+Brout, Sato, Guth, Starobinsky, Muchanov+Chibisov$

Brane worlds and early attempts

• String Theory D-branes offer a concrete, calculable realization of a brane universe.

Polchinski

• Branes in a cutoff-AdS₅ space were used to argue that this offers a context in which brane-world scales run exponentially fast, putting the hierarchy problem in a a very advantageous framework.

Randall+Sundrum

• It is in this context that the first attempts of "self tuning" of the brane cosmological constant were made.

Arkani-Hamed+Dimopoulos+Kaloper+Sundrum,Kachru+Schulz+Silverstein,

- The models used a (probe) bulk scalar to "absorb" the brane cosmological constant, and provide solutions with a flat brane metric despite the non-zero brane vacuum energy.
- The attempts failed as such solutions had invariantly a bad/naked bulk singularity that rendered models incomplete.

 More sophisticated setups were advanced and more general contexts have been explored but without success: the naked bulk singularity was always there.

Csaki+Erlich+Grojean+Hollowood,

 \bullet The Randall-Sundrum Z_2 orbifold boundary conditions were relaxed to consider even more general setups, but this did not improve the situation.

Padilla

• The RS setup and its siblings is related via holographic ideas to cutoff-CFTs and this provides independent intuition on the physics.

Maldacena, Witten, Arkani-Hamed + Porrati + Randall

- In view of our current understanding of holography, these failures were to be expected.
- Our goal: provide a 2.0 version of the self-tuning mechanism that is in line with the dictums of holography.

Emerged (Holographic) gravity and the SM

• We can envisage the physics of the SM+gravity (plus maybe other ingredients) as emerging from 4d UV complete QFTs:

Kiritsis

- a) A large N/strongly coupled stable (near-CFT)
- b) The Standard Model
- c) A massive sector of mass Λ , (the "messengers") that couples the two theories.
- (a) has a holographic description in a 5d space-time.
- For $E \ll \Lambda$ we can integrate out the "messenger" sector and obtain directly the SM coupled to the bulk gravity.
- The holographic picture is that of a brane (the SM) embedded in the bulk at $r \gtrsim \frac{1}{\Lambda}$.

- Holography reproduces the brane world embedded in a higher dimensional bulk.
- \bullet This picture has a UV cutoff: the messenger mass Λ .
- The configuration resembles string theory orientifolds and possible SM embeddings have been classified in the past.

Anastasopoulos+Dijkstra+Kiritsis+Schellekens

- The SM couples to all operators/fields of the bulk QFT.
- ullet Most of them they will obtain large masses of O(M) due to SM quantum effects.
- The only protected fields are the metric, the universal axion $\sim Tr[F \wedge F]$ and possible vectors (aka graviphotos).

1rst order RG flows

- We start by first describing the large-N QFT equations in a first order form. This is necessary later, in order to solve the Israel junction conditions.
- Consider a bulk (5d) Einstein-scalar theory (dual to the QFT dynamics of a scalar operator O(x) and the stress tensor $T_{\mu\nu}(x)$):

$$S_{bulk} = M^3 \int d^5x \sqrt{-g} \left[R - \frac{1}{2} (\partial \phi)^2 - V(\phi) \right]$$

and a Poincaré-invariant ansatz

$$ds^2 = du^2 + e^{2A(u)}(-dt^2 + d\vec{x}^2)$$
 , $\phi(u)$

- This describes the ground-state saddle point of a holographic RG flow (QFT).
- This will provide us flat brane solutions later.
- The independent bulk gravitational scalar-Einstein equations are

$$12\dot{A}(u)^2 - \frac{1}{2}\dot{\phi}^2 + V(\phi) = 0, \quad , \quad 6\ddot{A}(u) + \dot{\phi}^2 = 0,$$

They can be written as first order (holographic RG) flow equations

$$\dot{A}(u) := -\frac{1}{6}W(\phi) \quad , \quad \dot{\phi}(u) = W'(\phi)$$

in terms of the "superpotential" $W(\phi)$ that satisfies

$$V(\phi) = \frac{1}{2}W'^{2}(\phi) - \frac{1}{3}W^{2}(\phi)$$

- ullet The two systems are equivalent everywhere where $\dot{\phi} \neq 0$
- One of the integration constants is hidden in the non-linear superpotential equation but.....
- It is fixed, by asking the gravitational solution is regular at the interior of the space-time (IR in the QFT).
- The solutions are dual to RG flows from the UV (AdS boundary) to the IR (typically AdS if IR CFT) with (holographic) β -function

$$\frac{d\phi}{dA} = \beta(\phi) = -6\frac{d}{d\phi}\log W$$

• Conclusion: given a bulk action, the solution is characterized by the unique* superpotential function $W(\phi)$.

There are three integration constants in any solution:

- One appears in the $\dot{\phi}$ flow equation and is ϕ_0 ("the source") the value of the coupling dual to O in the UV of the dual QFT.
- ullet Another appears in the \dot{A} flow equation, and is A_0 an arbitrary length scale that sets the unit of length in the UV QFT.
- The third appears in W: it is the vev of the operator O in the ground state described by the solution: it is fixed by regularity in terms of ϕ_0 and A_0 .

Brane+Bulk equations

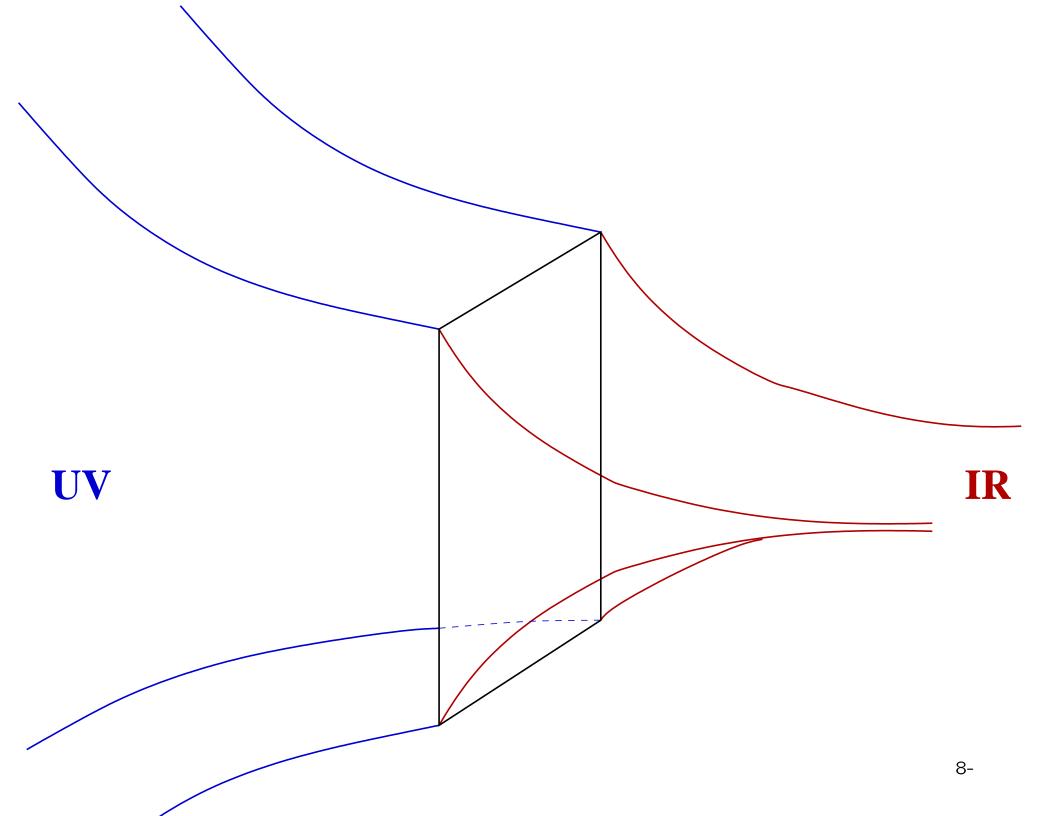
• We are ready to consider bulk solutions with the SM brane inserted at some radial position $u=u_0$.

$$S_{bulk} = M^3 \int d^5x \sqrt{-g} \left[R - \frac{1}{2} (\partial \Phi)^2 - V(\Phi) \right]$$

$$S_{brane} = M^2 \delta(u - u_0) \int d^4 x \sqrt{-\gamma} \left[W_B(\Phi) - \frac{1}{2} Z(\Phi) \gamma^{\mu\nu} \partial_{\mu} \Phi \partial_{\nu} \Phi + U(\Phi) R^B + \cdots \right]$$

- The \cdots above include the (renormalized) action of the Standard Model fields and their couplings to the bulk fields Φ and $g_{\mu\nu}$.
- The localized action on the brane is due to quantum effects of the SM fields.
- $W_B(\phi)$ is the cosmological term.

- The QFT setup indicates that the magnitude of W_B is of the order of the cutoff of the whole description, namely the messenger scale Λ .
- The brane is at a fixed radial position u_0 . This separates the bulk space into a part that contains the boundary (UV) and another (IR).
- The equations to solve are the bulk equations plus the Israel junction conditions at $u=u_0$.



- We denote by g_{ab}^{UV}, g_{ab}^{IR} and Φ^{UV}, Φ^{IR} the solutions for the metric and scalar field on each side of the brane.
- $\begin{bmatrix} X \end{bmatrix}_{UV}^{IR}$ is the jump of a quantity X across the defect.
- The Israel matching conditions are:
 - 1. Continuity of the metric and scalar field:

$$\left[g_{ab}\right]_{IR}^{UV} = 0, \qquad \left[\Phi\right]_{UV}^{IR} = 0$$

2. Discontinuity of the extrinsic curvature and normal derivative of Φ:

$$\left[K_{\mu\nu} - \gamma_{\mu\nu}K\right]_{UV}^{IR} = -\frac{1}{\sqrt{-\gamma}} \frac{\delta S_{brane}}{\delta \gamma^{\mu\nu}}, \qquad \left[n^a \partial_a \Phi\right]_{UV}^{IR} = \frac{\delta S_{brane}}{\delta \Phi},$$

ullet These conditions involve the first radial derivatives of A and Φ

 With the standard Poincaré invariant ansatz (with flat brane metric) we have

$$\dot{A}^{UV}(u) = -\frac{1}{6}W^{UV}(\Phi(u)), \qquad \dot{\Phi}^{UV}(u) = \frac{dW^{UV}}{d\Phi}(\Phi(u))$$

$$\dot{A}^{IR}(u) = -\frac{1}{6}W^{IR}(\Phi(u)), \qquad \dot{\Phi}^{IR}(u) = \frac{dW^{IR}}{d\Phi}(\Phi(u)).$$

ullet The scalar functions $W^{UV,IR}$ are both solutions to the superpotential equation:

$$\frac{1}{3}W^2 - \frac{1}{2}\left(\frac{dW}{d\Phi}\right)^2 = V.$$

The continuity conditions are

$$A^{UV}(u_0) = A^{IR}(u_0) = A_0, \qquad \Phi^{UV}(u_0) = \Phi^{IR}(u_0) = \Phi_0.$$

- Only one initial condition (A_*, Φ_*) must be imposed in the UV and this choice corresponds to the (relevant) coupling of the bulk CFT.
- The jump conditions are

$$W^{IR} - W^{UV}\big|_{\Phi_0} = W^B(\Phi_0) \quad , \quad \frac{dW^{IR}}{d\Phi} - \frac{dW^{UV}}{d\Phi}\big|_{\Phi_0} = \frac{dW^B}{d\Phi}(\Phi_0)$$

Old Self-Tuning

• W_{UV} and W_{IR} are determined from the superpotential equation up to one integration constant, C_{UV}, C_{IR} .

• For a generic brane potential $W^B(\Phi)$, the two matching equations

$$W^{IR} - W^{UV} \Big|_{\Phi_0} = W^B(\Phi_0) \quad , \quad \frac{dW^{IR}}{d\Phi} - \frac{dW^{UV}}{d\Phi} \Big|_{\Phi_0} = \frac{dW^B}{d\phi}(\Phi_0)$$

will fix C^{UV} , C^{IR} for any generic value of Φ_0 .

- ullet The fixed value of C_{IR} typically leads to a bad IR singularity.
- Moreover Φ_0 is a modulus and generates a massless mode (the radion).

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- ullet The IR constant C^{IR} should be fixed by demanding that the IR singularity is absent.
- Typically there is only one such solution to the superpotential equation (or a discreet set).
- ullet According to holography rules, the solution W^{IR} should be fixed before we impose the matching conditions.
- \bullet Once W^{IR} is fixed by regularity, the Israel conditions will determine:
- \spadesuit The integration constant C^{UV} in the UV superpotential
- \spadesuit The brane position in field space, Φ_0 .
- This is a desirable outcome as there would be no massless radion mode.
- It can be checked that generically such an equilibrium position exists.

To recapitulate:

- We have shown that generically, a flat brane solution exists irrespective of the details of the "cosmological constant" function $W_B(\Phi)$
- The position of the brane in the bulk, determined via Φ_0 , is fixed by the dynamics. There is typically a single such equilibrium position.
- This is good news, but we are still far from "solving" the cosmological constant problem.
- We must analyze the stability of such an equilibrium position.
- We must analyze the nature of gravity and the equivalence principle on the brane.

Linear perturbations around a flat brane

- We investigate the dynamics of bulk fluctuations equations.
- There are several fluctuations that originate in the bulk metric.
- There is a scalar fluctuation due to the bulk scalar, Ф.
- Before we insert a brane in the bulk, it is known that there are two non-trivial (propagating) fluctuations: $\hat{h}_{\mu\nu}$ and a scalar mode ζ .
- The physical bulk scalar can be identified with the gauge-invariant combination:

$$\zeta = \psi - \frac{A'}{\phi_o'}\chi.$$

- In the presence of the brane there is also the embedding mode $X^A(\sigma^{\alpha})$.
- We choose the static gauge, so the embedding is completely specified by the radial profile $r(x^{\mu})$.
- We consider a small deviation from the equilibrium position r_0 :

$$r(x^{\mu}) = r_0 + \rho(x^{\mu})$$

• The brane scalar mode ρ is known as the brane bending mode.

Induced gravity

- We proceed to solve the fluctuation equations:
- The tensor mode satisfies the Laplacian equation in the bulk

$$\partial_r^2 \hat{h}_{\mu\nu} + (d-1)(\partial_r A)\partial_r \hat{h}_{\mu\nu} + \partial^\rho \partial_\rho \hat{h}_{\mu\nu} = 0$$

and the matching condition

$$\left[\hat{h}'_{IR} - \hat{h}'_{UV}\right]_{r_0} = -U(\phi_0) \quad e^{-A_0} \quad \partial^{\mu}\partial_{\mu}\hat{h}(r_0),$$

• This is a condition similar to DGP but instead of flat space we are in a non-trivial bulk metric.

Dvali+Gabadadze+Porrati

The gravitational interaction on the brane

The field equations together with the matching conditions can be obtained by extremizing

$$S[h] = M^{d-1} \int d^dx dr \sqrt{-g} g^{ab} \partial_a \hat{h} \partial_b \hat{h} + M^{d-1} \int_{r=r_0} d^dx \sqrt{\gamma} \ U^B(\phi) \gamma^{\mu\nu} \partial_\mu \hat{h} \partial_\nu \hat{h},$$

where $g_{ab}=e^{A(r)}\eta_{ab}$ and $\gamma_{\mu\nu}=e^{A_0}$ $\eta_{\mu\nu}$ are the unperturbed bulk metric and induced metric on the brane, respectively.

We introduce brane-localized matter sources,

$$S_m = \int d^d x \sqrt{\gamma} \ \mathcal{L}_m(\gamma_{\mu\nu}, \psi_i)$$

where ψ_i denotes collectively the matter fields.

ullet The interaction of brane stress tensor $T_{\mu\nu}$ can be written in terms of the propagator G:

$$S_{int} = -\frac{e^{4A_0}}{2M^3} \int d^4x d^4x' \ G(r_0, x; r_0, x') \left(T_{\mu\nu}(x) T^{\mu\nu}(x') - \frac{1}{3} T_{\mu}{}^{\mu}(x) T_{\nu}{}^{\nu}(x') \right)$$

- Notice that the combination above is appropriate for a massive graviton exchange
- The metric on the brane after a rescaling is the flat metric $\gamma_{\mu\nu}=\eta_{\mu\nu}$.
- The brane-to-brane propagator in momentum space $(G(r_0, x; r_0, x') \rightarrow G(p))$ is given by:

$$G(p) = -\frac{1}{M^3} \quad \frac{D(p, r_0)}{1 + [U_0 D(p, r_0)]p^2}$$

where D(p,r) is the bulk to bulk propagator.

When

$$U_0 \ D(p, r_0) \ p^2 \gg 1 \ , \ G(p) \simeq - \ \frac{1}{M^3 U_0} \ \frac{1}{p^2}$$

the propagator is 4-dimensional and

$$M_P^2 = U_0 M^3$$

• D(p,r) is determined by the Laplacian in the UV and IR part of the geometry, with continuity and unit jump at the brane.

- ullet The 4-d phase is always present at large enough and at low enough p^2 .
- The crossover scale is determined by the equation:

$$U_0 p^2 D(p, r_0) = 1$$

The characteristic scales

- There are the following characteristic distance scales that play a role, besides r_0 .
- The transition scale r_t around which $D(r_0, p)$ changes from small to large momentum asymptotics:

- \bullet The transition scale r_t depends on r_0 and the bulk QFT dynamics.
- \bullet The *crossover scale*, or DGP scale, r_c :

$$r_c \equiv \frac{U_0}{2};$$

This scale determines the crossover between 5-dimensional and 4-dimensional behavior, and enters the 4D Planck scale and the graviton mass.

• The gap scale d_0

$$d_0 \equiv D(r_0, 0) = \int_0^{r_0} dr' e^{-3A_{UV}(r')},$$

which governs the propagator at the largest distances (in particular it sets the graviton mass as we will see).

- Typically, $d_0 \lesssim r_0$
- ullet For example, in IR AdS we have

$$d_0 \simeq \frac{r_0}{4}$$

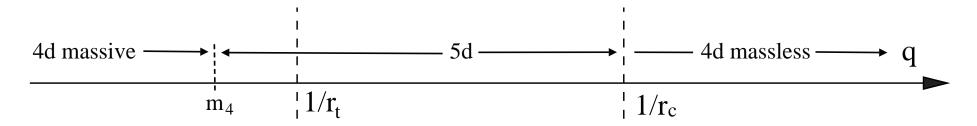
In confining bulk backgrounds we have instead

$$d_0 \simeq \frac{1}{6\Lambda^2 r_0}$$

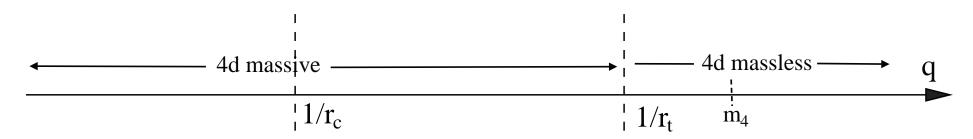
• In the far IR, $\Lambda r_0 \gg 1$ and d_0 can be made arbitrarily small.

Massive gravity on the brane

• When $r_t > r_c$ we have three regimes for the gravitational interaction on the brane:



- Massive 4d gravity $(r_t < r_c)$
- ullet In this case, at all momenta above the transition scale, $p\gg 1/r_t>1/r_c$, we are in the 4-dimensional regime of the DGP-like propagator.



 The behavior is four-dimensional at all scales, and it interpolates between massless and massive four-dimensional gravity.

Kiritsis+Tetradis+Tomaras

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More on scales

- Some scales depend on the bulk dynamics—the nature of the RG flow.
- Some others depend on boundary conditions = the UV coupling constant
- The two important parameters for 4d gravity depend as follows on b.c.

$$\frac{m_0}{M_P} \sim \left(\frac{M}{\Lambda}\right)^2 \frac{1}{N_3^2} \quad , \quad m_0 \ M_P = \left(\frac{M^3}{d_0}\right)^{\frac{1}{2}}$$

- d_0 depends only on the bulk theory.
- The choice of a small ratio $\frac{m_0}{M_P}\sim 10^{-60}$ is (technically) natural from the QFT point of view.

Scalar Perturbations

- The next step is to study the scalar perturbations. They are of interest as they might destroy the equivalence principle.
- The equations for the scalar perturbations can be derived and they are complicated.
- Unlike previous analysis of similar systems they cannot be factorized to a relatively simple system as the graviton.
- There are two scalar modes on the brane:
- In one gauge, the brane bedding mode can be "eliminated" but the scalar perturbation is discontinuous on the brane.
- In another gauge the perturbation is continuous but the brane bending mode is present.

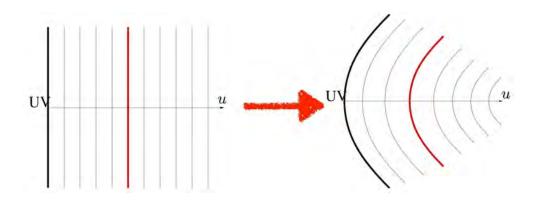
- In general the two scalar modes couple to two charges: the "scalar charge" and the trace of the brane stress tensor.
- The mode that couples to the scalar charge has a "heavy" mass of the order of the cutoff.
- \bullet The mode that couples to the trace of the stress-tensor has a mass that is O(1) in cutoff units (like the graviton mass).
- All the stability conditions for the scalars depend on more details of the brane induced functions $W_B(\Phi)$, $U_B(\Phi)$, $Z_B(\Phi)$.
- They can be investigated further from the known parameter dependence of the vacuum energy.

 Kounnas+Pavel+Zwirner, Dimopoulos+Giudince+Tetradis
- There is a vDVZ discontinuity that (as usual) cannot be cancelled at the linearized order, if the theory is positive.
- It should be cancelled by the Vainstein mechanism. To derive the relevant constraints on parameters, we must study non-linear solutions of sources on the brane.

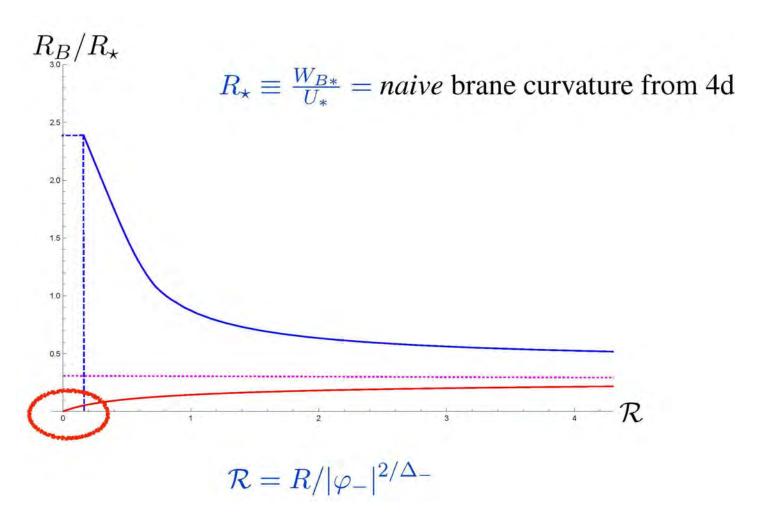
dS or AdS solutions on the brane

- We may ask also the question: Can we obtain solutions where the brane has not trivial curvature, ie dS_4 or AdS_4 ?
- \bullet It can be shown that with the (AdS₅) boundary condition for the metric to be flat, this is generically impossible.
- it becomes possible if the boundary condition for the metric is dS_4 or AdS_4 , ie. the quantum field theory dual to the bulk gravitational theory lives on dS_4 or AdS_4 .
- Then the bulk ansatz can be parametrized as

$$ds^{2} = du^{2} + e^{2A(u)}\zeta_{\mu\nu}dx^{\mu}dx^{\nu}$$
 , $\Phi(u)$



- ullet We have developed the formalism to solve for holographic RG flows for QFTs on constant curvature manifolds.
- We can then find solutions where the brane is "self-tuning" but curved.



For a Mex-hat bulk potential and exponential $W_B(\Phi)$ and $U(\Phi)$.

The cosmology of self-tuning branes

- The existence of self-tuning solutions is only a first step towards addressing the cosmological constant problem.
- The general problem to solve is the time dependent problem where the brane is moving away from the equilibrium point.
- This problem is difficult to solve as in such a case both the bulk solution and the brane are time dependent.
- We will try the probe approximation as it is solvable and can give useful intuition on what happens.
- In such a case, the brane moves in a fixed bulk solution. Its motion generates cosmology on the brane = mirage cosmology.

Kehagias+Kiritsis

 For a standard Lorentz-invariant bulk solution, the induced brane metric is

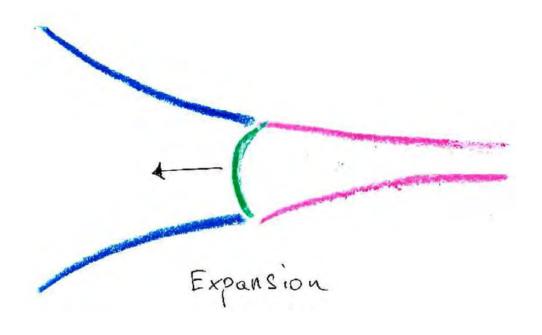
$$ds_{brane}^2 = (\dot{u}^2 - e^{2A(u)}) dt^2 + e^{2A(u)} d\vec{x}^2 = -d\tau^2 + e^{2A} d\vec{x}^2$$

where u(t) is the brane position that is now a function of time and the brane cosmic time is defined as

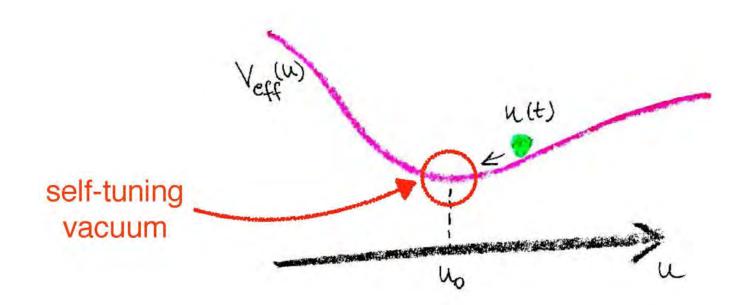
$$d\tau = \sqrt{e^{2A} - \dot{u}^2} \ dt$$

while the brane Hubble constant is

$$H^{2} \equiv \left(\frac{dA}{d\tau}\right)^{2} = A'^{2} \frac{\dot{u}^{2} e^{-2A}}{1 - \dot{u}^{2} e^{-2A}}$$

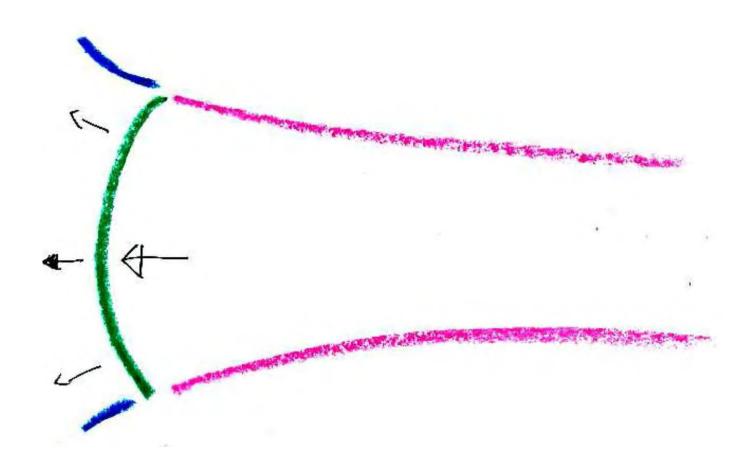


• The brane trajectory u(t) can be found by integrating the analogue of the geodesic equations, that can be integrated once at the cost of introducing an integration constant E, ("energy").

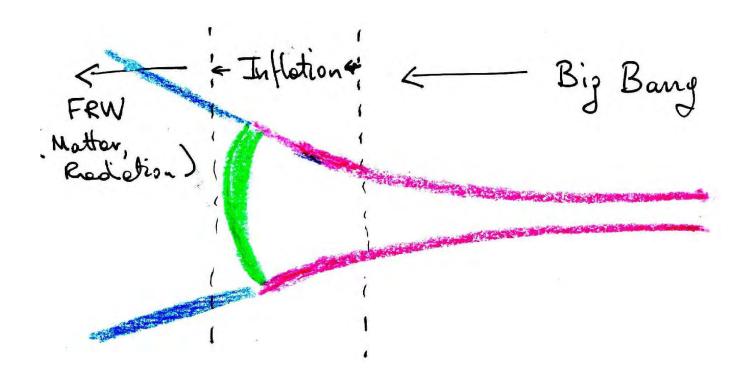


- In the non-relativistic limit, the equations are those of a particle in a potential.
- The minima are where the self-tuning solutions lie.

When the brane moves near the boundary, the brane geometry is dS



$$u(\tau) = \ell H_{eff} \tau$$
 , $H_{eff} = \sqrt{\frac{W_B}{U_B}} \Big|_{boundary}$



- Early universe inflation can happen in an intermediate near-AdS region ("walking" bulk theory).
- In such a case $\epsilon << 1$ but η requires further study.

Hamada+Kiritsis+Nitti

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Connecting the Hierarchy Problem

• We can include the Higgs scalar in the effective potential on the brane:

$$S_{Higgs} = M_p^2 \int d^d x \sqrt{-\gamma} \left[-X(\Phi) |\mathbf{H}|^2 - S(\Phi) |\mathbf{H}|^4 + T(\Phi) R |\mathbf{H}|^2 + \cdots \right]$$

We must also add the equations of motion for the Higgs:

$$(X(\Phi) + 2S(\Phi)|H|^2) H = 0$$

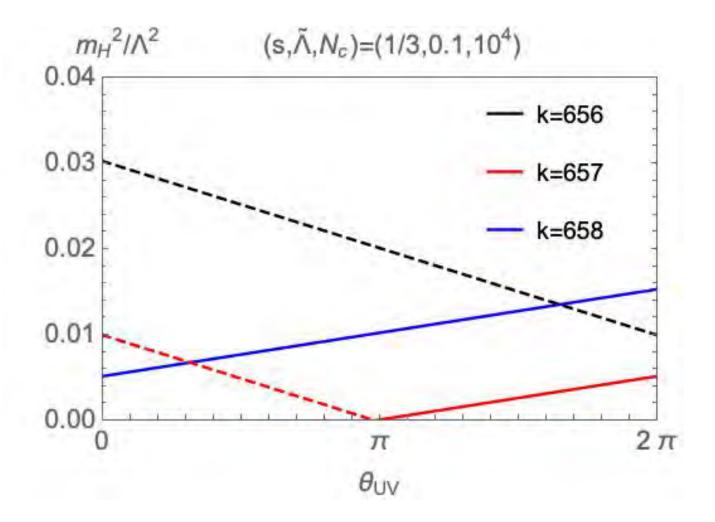
- Whether the hierarchy problem is solved at the self-tuning position relies on whether $X(\Phi_0) \ll \Lambda$.
- Typically, there is no reason for this to happen.
- Unless there is another bulk field a, so that $X(a, \Phi)$ and there are multiple solutions for a the make X scan.
- A bulk field with such a property is an axion (=holographic relaxion).

Holographic axions

- They are dual to instanton density operator.
- They have no perturbative bulk potential
- ullet Their source near the AdS-like boundary is related to the heta-angle of the dual QFT as

$$a(u) = a_{UV} + Qe^{-4\frac{u}{\ell}} + \cdots$$
, $a_{UV} = c\frac{\theta + 2\pi k}{N_c}$, $k \in \mathbb{Z}$

- ullet It can be shown that the range of a_{UV} is finite.
- Therefore for given θ there is a large $O(N_c)$ number of saddle points with different values of a_{UV} .
- These different solutions give different Higgs masses and can make $X(a, \Phi)$ vanish.



• Like the relaxion model, it is not clear yet, how to make the parameters in $X(a, \Phi)$ "natural".

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Conclusions and Outlook

- A large-N QFT coupled holographically to the SM offers the possibility of tuning the SM vacuum energy.
- The graviton fluctuations have DGP behavior while the graviton is massive at large enough distances.
- No unnatural tuning is needed to have a reasonable Planck scale. The graviton mass can be very small in a natural fashion as well.
- There are however many extra constraints that need to be analyzed in detail:
- Constraints from the healthy behavior of scalar modes. Constraints from the equivalence principle and the Vainshtein mechanism
- The cosmological evolution must be completed by adding the rest of the ingreedients
- And the solution to the hierarchy problem needs a good origin of the function X and a mechanism to arrive at the right solution.

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THANK YOU

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A simple numerical example

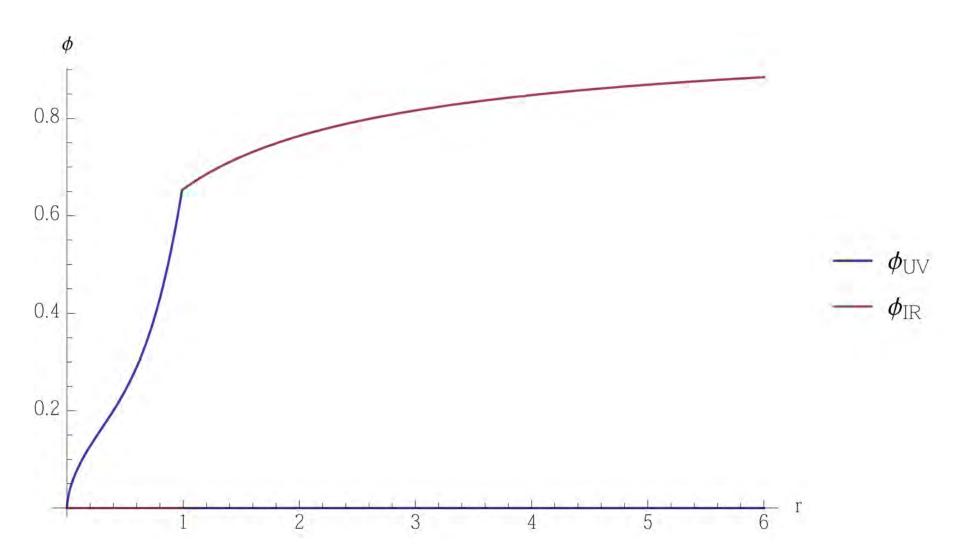
$$V(\phi) = -12 + \frac{1}{2} \left(\phi^2 - 1\right)^2 - \frac{1}{2},$$

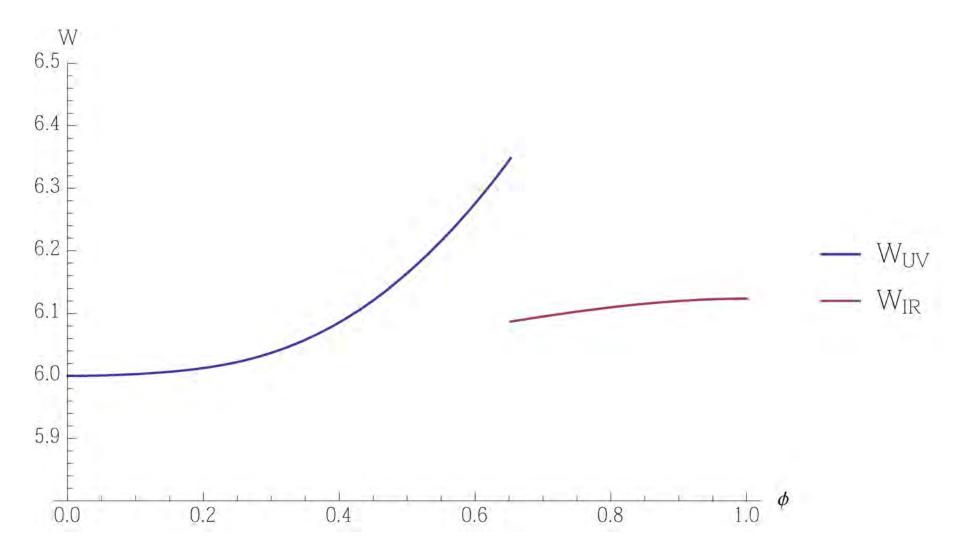
• The flow is from $\phi = 0$ (UV Fixed point) to $\phi = 1$ (IR fixed point).

$$W_b(\phi) = \omega \exp[\gamma \phi].$$

$$\omega = -0.01, \ \gamma = 5 \qquad \Rightarrow \qquad \phi_0 = 0.65.$$

• This gives, in conformal coordinates, $r_0 = 0.99$.





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The bulk propagator

ullet At large Euclidean p^2 , we can approximate the bulk equations as in flat space,

$$\partial_r^2 \Psi^{(p)}(r) = p^2 \Psi^{(p)}(r)$$

except for small r, where the effective Schrödinger potential is $\sim 1/r^2$ and cannot be neglected.

ullet The solution satisfying appropriate boundary conditions (vanishing in the IR and for r o 0) and jump condition is

$$\Psi_{IR}^{(p)} = \frac{\sinh pr_0}{p} e^{-pr}, \quad \Psi_{UV}^{(p)} = \frac{e^{-pr_0}}{p} \sinh pr, \qquad p \equiv \sqrt{p^2}$$

 \bullet For large p, it is like in flat 5d space

$$D(p, r_0) = \frac{\sinh p r_0}{p} e^{-pr_0} \simeq \frac{1}{2p}, \qquad pr_0 \gg 1$$

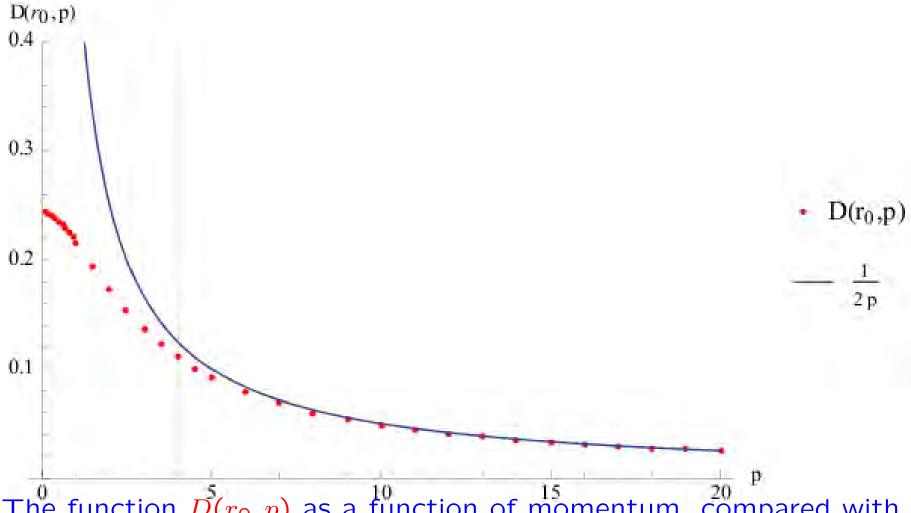
• At small momenta the bulk propagator has always an expansion in powers of p^2 and we can solve perturbatively in p^2 .

- ullet If the geometry is gapped, the expansion is analytic in p^2
- ullet If the geometry is gapless, then after some power of p non-analyticities appear.
- We find that as $p \to 0$

$$D(p,r) = d_0 + d_2 p^2 + d_4 p^4 + \cdots$$

The coefficients d_i can be explicitly computed from the bulk unperturbed solution. For example

$$d_0 = e^{3A_0} \int_0^{r_0} dr' e^{-3A_{UV}(r')}$$



The function $D(r_0, p)$ as a function of momentum, compared with 1/2p. The transition scale $1/r_t$ (solid line) is about 4 (in UV-AdS units)

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Scalar Perturbations

The perturbations are

$$ds^2 = a^2(r) \left[(1+2\phi)dr^2 + 2A_\mu dx^\mu dr + (\eta_{\mu\nu} + h_{\mu\nu})dx^\mu dx^\nu \right], \quad \varphi = \bar{\varphi}(r) + \chi$$
 and the scalar ones are

$$\phi$$
, χ , $A_{\mu} = \partial_{\mu}B$, $h_{\mu\nu} = 2\psi\eta_{\mu\nu} + 2\partial_{\mu}\partial_{\nu}E$,

plus the brane-bending mode $\rho(x)$ defined as

$$r(x^{\mu}) = r_0 + \rho(x^{\mu})$$

• Unlike the tensor modes, these fields are not gauge-invariant. Under an infinitesimal diff transformation $(\delta r, \delta x^{\mu}) = (\xi^5, g^{\mu\nu}\partial_{\nu}\xi)$ they transform as

$$\delta\psi = -\frac{a'}{a}\xi^5 \quad , \quad \delta\phi = -(\xi^5)' - \frac{a'}{a}\xi^5 \quad , \quad \delta B = -\xi' - \xi^5$$
$$\delta E = -\xi \quad , \quad \delta\chi = -\bar{\varphi}'\xi^5 \quad , \quad \delta\rho = \xi^5(r_0, x).$$

• We partly fix the gauge by choosing B = 0.

- \bullet We are still free to do radial gauge-transformations and r-independent space-time diffeomorphisms and keep this gauge choice.
- The matching conditions become

$$\left[a^{2}(r_{0}+\rho)\left(2\psi\eta_{\mu\nu}+2\partial_{\mu}\partial_{\nu}E\right)\right]_{IR}^{UV}=0, \qquad \left[\bar{\varphi}(r_{0}+\rho)+\chi\right]_{UV}^{IR}=0$$
$$\left[\hat{\psi}\right]_{IR}^{UV}=0, \qquad \left[\hat{\chi}\right]_{IR}^{UV}=0, \qquad \left[E\right]_{UV}^{IR}=0$$

where we have defined the new bulk perturbations:

$$\widehat{\psi}(r,x) = \psi + A'(r)\rho(x), \quad \widehat{\chi}(r,x) = \chi + \overline{\varphi}'(r)\rho(x) \quad , \quad A' = a'/a$$

The gauge-invariant scalar perturbation has the same expression in terms of these new continues variables:

$$\zeta = \psi - \frac{A'}{\bar{\varphi}'}\chi = \hat{\psi} - \frac{A'}{\bar{\varphi}'}\hat{\chi}.$$

In general however $\zeta(r,x)$ is not continuous across the brane, since the background quantity $A'/\bar{\varphi}'$ jumps:

$$\left[\zeta\right]_{IR}^{UV} = \left[\frac{A'}{\bar{\varphi}'}\right]_{IR}^{UV} \hat{\chi}(r_0)$$

Notice that this equation is gauge-invariant since, under a gauge transformation:

$$\delta \widehat{\chi}(r,x) = -\overline{\varphi}'(r) \left[\xi^{5}(r,x) - \xi^{5}(r_{0},x) \right],$$

thus $\hat{\chi}(r_0)$ on the right hand side of equation (??) is invariant.

It is convenient to fix the remaining gauge freedom by imposing:

$$\chi(r,x)=0.$$

To do this, one needs different diffeomorphisms on the left and on the right of the brane, since $\bar{\varphi}'$ differs on both sides. The continuity for $\hat{\chi}$ then becomes the condition:

$$\rho_{UV}(x)\bar{\varphi}'_{UV}(r_0) = \rho_{IR}(x)\bar{\varphi}'_{IR}(r_0)$$

i.e. the brane profile looks different from the left and from the right. This is not a problem, since equation (??) tells us how to connect the two sides given the background scalar field profile.

In the $\chi = 0$ gauge we have:

$$\zeta = \psi = \hat{\psi} - A'\rho, \qquad \hat{\chi}(r_0) = \bar{\varphi}'(r_0)\rho.$$

This makes it simple to solve for ϕ using the bulk constraint equation (in particular, the $r\mu$ -component of the perturbed Einstein equation, for the details see the Appendix:

$$\phi = \frac{a}{a'}\psi' = \frac{a}{a'}\hat{\psi}' + \left(\frac{a'}{a} - \frac{a''}{a}\right)\rho$$

where it is understood that this relation holds both on the UV and IR sides.

In the gauge $\chi=B=0$, the second matching conditions to linear order in perturbations, read

$$\left[(1 - d)a'(r_0) \left(2\hat{\psi} \eta_{\mu\nu} + 2\partial_{\mu}\partial_{\nu}E \right) + \frac{1}{2}a(r_0)(\bar{\varphi}')^2 \rho \eta_{\mu\nu} + \left(\partial_{\mu}\partial_{\nu} - \eta_{\mu\nu}\partial^{\sigma}\partial_{\sigma} \right) \left(E' - \rho \right) \right]_{UV}^{IR} = \frac{a^2(r_0)}{2} W_B(\Phi_0) \left(2\eta_{\mu\nu}\hat{\psi} + 2\partial_{\mu}\partial_{\nu}E \right)_{r_0} + \frac{a^2(r_0)}{2} dW_B(\Phi_0) \left(2\eta_{\mu\nu}\hat{\psi} + 2\partial_$$

$$\frac{a^{2}(r_{0})}{2}\frac{dW_{B}}{d\varphi}\Big|_{\Phi_{0}}\bar{\varphi}'(r_{0})\rho - (d-2)U_{B}(\Phi_{0})\left(\partial_{\mu}\partial_{\nu} - \eta_{\mu\nu}\partial^{\sigma}\partial_{\sigma}\right)\hat{\psi},$$

$$\left[\frac{\bar{\varphi}'}{a'}\hat{\psi}' + \left(\frac{(\bar{\varphi}')^2}{6a'} - \frac{\bar{\varphi}''}{a\bar{\varphi}'}\right)\bar{\varphi}'\rho\right]_{UV}^{IR} =$$

$$= -\frac{d^2W_B}{d\Phi^2}\Big|_{\Phi_0} \bar{\varphi}'\rho + \frac{Z_B(\Phi_0)}{a^2} \bar{\varphi}'\partial^\sigma \partial_\sigma \rho - \frac{2(d-1)}{a^2} \frac{dU_B}{d\Phi}\Big|_{\Phi_0} \partial^\sigma \partial_\sigma \hat{\psi}$$

Using the background matching conditions in conformal coordinates,

$$\frac{a'}{a^2} = -\frac{1}{2(d-1)}W, \qquad \bar{\varphi}' = a\frac{dW}{d\Phi},$$

one can see that the first two terms on each side cancel each other, and we are left with an equation that fixes the matching condition for E'(r,x):

$$\left[E'-\rho\right]_{UV}^{IR} = -2\frac{U_B(\Phi_0)}{a(r_0)}\widehat{\psi}(r_0).$$

$$\left[\hat{\psi}\right]_{UV}^{IR}=0$$
;
$$\left[\bar{\varphi}'\rho\right]_{UV}^{IR}=0$$
;

$$\left[\frac{\bar{\varphi}'a}{a'}\hat{\psi}'\right]_{UV}^{IR} = \left[\left(\frac{Z_B(\Phi_0)}{a}\partial^{\mu}\partial_{\mu} - \mathcal{M}_b^2\right)\bar{\varphi}'\rho - \frac{6}{a}\frac{dU_B}{d\Phi}(\Phi_0)\partial^{\mu}\partial_{\mu}\hat{\psi}\right]_{r_0}$$

where we have defined the brane mass:

$$\mathcal{M}_b^2 \equiv a(r_0) \frac{d^2 W_b}{d\Phi^2} \Big|_{\Phi_0} + \left[\left(\frac{(\bar{\varphi}')^2}{6} \frac{a}{a'} - \frac{\bar{\varphi}''}{\bar{\varphi}'} \right) \right]_{UV}^{IR}.$$

Using the background Einstein's equations this can also be written as:

$$\mathcal{M}_b^2 = \left[\frac{a'}{a} - \frac{a''}{a'}\right]_{UV}^{IR} + a\left(\frac{d^2W_B}{d\Phi^2} - \left[\frac{d^2W}{d\Phi^2}\right]_{UV}^{IR}\right),$$

We can eliminate E

$$\Box E' = -\frac{a}{a'} \left[\Box \psi + \frac{a}{a'} \left(2 \frac{a'^2}{a^2} - \frac{a''}{a} \right) \psi' \right].$$

Notice that the combination multiplying ψ' can be written as $(a/a')(\bar{\varphi}')^2/6$.

The bulk equation for ζ ($\equiv \psi$ in this gauge) on both sides of the brane is:

$$\psi'' + \left(3\frac{a'}{a} + 2\frac{z'}{z}\right)\psi' + \partial^{\mu}\partial_{\mu}\psi = 0,$$

where $z = \bar{\varphi}' a / a'$.

To summarize, we arrive at the following equations and matching conditions, either in terms of ψ :

$$\psi'' + \left(3\frac{a'}{a} + 2\frac{z'}{z}\right)\psi' + \partial^{\mu}\partial_{\mu}\psi = 0,$$

$$\left[\psi\right]_{UV}^{IR} = -\left[\frac{a'}{a\bar{\varphi}'}\right]_{UV}^{IR}\bar{\varphi}'\rho, \qquad \left[\bar{\varphi}'\rho\right]_{UV}^{IR} = 0;$$

$$\left[\frac{a^2}{a'^2}\frac{\bar{\varphi}'^2}{6}\psi'\right]_{UV}^{IR} = \left(\frac{2U_B(\Phi_0)}{a} - \left[\frac{a}{a'}\right]_{UV}^{IR}\right)\Box\left(\psi + \frac{a'}{a}\rho\right);$$

$$\left[\frac{a\bar{\varphi}'}{a'}\psi'\right]_{UV}^{IR} = -6\frac{dU_B}{d\Phi}(\Phi_0)\Box\left(\psi + \frac{a'}{a}\rho\right) + \left(\frac{Z_B(\Phi_0)}{a}\Box - \tilde{\mathcal{M}}_b^2\right)\bar{\varphi}'\rho;$$

$$\Box \equiv \partial^{\mu}\partial_{\mu}, \quad z \equiv \frac{a\bar{\varphi}'}{a'}, \quad \tilde{\mathcal{M}}_b^2 = a\left(\frac{d^2W_B}{d\Phi^2} - \left[\frac{d^2W}{d\Phi^2}\right]_{UV}^{IR}\right).$$

ullet in terms of $\widehat{\psi}$:

$$\begin{split} \hat{\psi}'' + \left(3\frac{a'}{a} + 2\frac{z'}{z}\right)\hat{\psi}' + \partial^{\mu}\partial_{\mu}\hat{\psi} &= \mathcal{S}, \\ \left[\hat{\psi}\right]_{UV}^{IR} &= 0, \qquad \left[\bar{\varphi}'\rho\right]_{UV}^{IR} &= 0; \\ \left[\frac{a^2}{a'^2}\frac{\bar{\varphi}'^2}{6}\hat{\psi}'\right]_{UV}^{IR} &= -\left[\frac{\bar{\varphi}'}{6}\left(\frac{a''a}{a'^2} - 1\right)\right]_{UV}^{IR}\bar{\varphi}'\rho + \left(\frac{2U_B(\Phi_0)}{a} - \left[\frac{a}{a'}\right]_{UV}^{IR}\right)\Box\hat{\psi}; \\ \left[\frac{a\bar{\varphi}'}{a'}\hat{\psi}'\right]_{UV}^{IR} &= -6\frac{dU_B}{d\Phi}(\Phi_0)\Box\hat{\psi} + \left(\frac{Z_B(\Phi_0)}{a}\Box - \mathcal{M}_b^2\right)\bar{\varphi}'\rho; \\ \Box &\equiv \partial^{\mu}\partial_{\mu}, \qquad z \equiv \frac{a\bar{\varphi}'}{a'}, \qquad \mathcal{M}_b^2 = \tilde{\mathcal{M}}_b^2 + \left[\frac{a'}{a} - \frac{a''}{a'}\right]_{UV}^{IR}, \\ \mathcal{S} \equiv A'''\rho + 3(A' + 2z'/z)A''\rho + A'\Box\rho. \end{split}$$

remarks:

- In both formulations there are 6 parameters in the system: 4 in the bulk (2 integration constants in the UV, 2 in the IR) and 2 brane parameters (ρ on each side). From these 6 we can subtract one: a rescaling of the solution, which is not a true parameter since the system is homogeneous in (ρ, ψ) . There is a total of 4 matching conditions, plus 2 normalizability conditions if the IR is confining, or only one if it is not. Thus, in the confining case, we should find a quantization condition for the mass spectrum, whereas in the non-confining case the spectrum is continuous and the solution unique given the energy. The goal will be to show that such solutions exist only for positive values of m^2 , defined as the eigenvalue of \square . To see this, one must go to the Schrodinger formulation.
- Notice that something interesting happens when the *second* derivative of the brane potential matches the discontinuity in the second derivative of the bulk superpotential: in that case the brane mass term for ρ vanishes. For a generic brane potential of course this is not the case, but it happens for example in fine-tuned models when the brane position is not fixed by the zeroth-order matching conditions, for example when the brane potential is chosen to be equal to the bulk superpotential, and a Z_2 symmetry is imposed. This is the generalization of the RS fine-tuning in the presence of a bulk scalar. The fact that the mass term vanishes in this case must be related to the presence of zero-modes (whether they are normalizable or not is a different story).

To put the matching conditions in a more useful form, it is convenient to eliminate $\rho_{L,R}$ altogether :

$$\left[\frac{a'}{a}\rho\right] = -[\psi], \qquad [\bar{\varphi}'\rho] = 0$$

These can be solved to express the continuous quantities $\hat{\psi}(0)$ and $\bar{\varphi}'\rho$ in terms of $\psi_{L,R}$ only:

$$\widehat{\psi}(0) = \frac{[z\,\psi]}{[z]}, \qquad \overline{\varphi}'\rho = -\frac{[\psi]}{[1/z]}, \qquad z = \frac{a\overline{\varphi}'}{a'}$$

Using these results, we obtain a relation between the left and right functions and their derivatives:

$$[z\psi'] = -6\frac{dU_B}{d\Phi} \Box \frac{[z\,\psi]}{[z]} - \frac{1}{a} \left(Z_B \Box - a^2 \tilde{M}^2 \right) \frac{[\psi]}{[z^{-1}]}$$

$$[z^2\psi'] = 6 \left(2\frac{U_B}{a} - \left[\frac{a}{a'} \right] \right) \Box \frac{[z\,\psi]}{[z]}$$

Since the left hand side is in general non-degenerate, these equations can be solved to give ψ_L' and ψ_R' as linear combinations of ψ_L and ψ_R ,

$$\begin{pmatrix} \psi_L'(0) \\ \psi_R'(0) \end{pmatrix} = \Gamma \begin{pmatrix} \psi_L(0) \\ \psi_R(0) \end{pmatrix}$$

with a suitable matrix Γ .

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RG

• $W(\phi)$ is the non-derivative part of the Schwinger source functional of the dual QFT =on-shell bulk action.

de Boer+Verlinde²

$$S_{on-shell} = \int d^d x \sqrt{\gamma} \ W(\phi) + \cdots \Big|_{u \to u_{IIV}}$$

The renormalized action is given by

$$S_{renorm} = \int d^d x \sqrt{\gamma} \left(W(\phi) - W_{ct}(\phi) \right) + \cdots \Big|_{u \to u_{UV}} =$$

$$= constant \int d^{d}x \ e^{dA(u_{0}) - \frac{1}{2(d-1)} \int_{\phi_{U}V}^{\phi_{0}} d\tilde{\phi}_{W}^{W'}} + \cdots$$

- \bullet The statement that $\frac{dS_{renorm}}{du_0}=0$ is equivalent to the RG invariance of the renormalized Schwinger functional.
- It is also equivalent to the RG equation for ϕ .

We can show that

$$T_{\mu}{}^{\mu} = \beta(\phi) \langle O \rangle$$

• The Legendre transform of S_{renorm} is the (quantum) effective potential for the vev of the QFT operator O.

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Detour: The local RG

• The holographic RG can be generalized straightforwardly to the local RG

$$\dot{\phi} = W' - f' R + \frac{1}{2} \left(\frac{W}{W'} f' \right)' (\partial \phi)^2 + \left(\frac{W}{W'} f' \right) \Box \phi + \cdots$$

$$\dot{\gamma}_{\mu\nu} = -\frac{W}{d-1}\gamma_{\mu\nu} - \frac{1}{d-1}\left(f R + \frac{W}{2W'}f'(\partial\phi)^2\right)\gamma_{\mu\nu} +$$

$$+2f R_{\mu\nu} + \left(\frac{W}{W'}f' - 2f''\right)\partial_{\mu}\phi\partial_{\nu}\phi - 2f'\nabla_{\mu}\nabla_{\nu}\phi + \cdots$$

Kiritsis+Li+Nitti

• $f(\phi)$, $W(\phi)$ are solutions of

$$-\frac{d}{4(d-1)}W^2 + \frac{1}{2}W'^2 = V \quad , \quad W' f' - \frac{d-2}{2(d-1)}W f = 1$$

• Like in 2d σ -models we may use it to define "geometric" RG flows.

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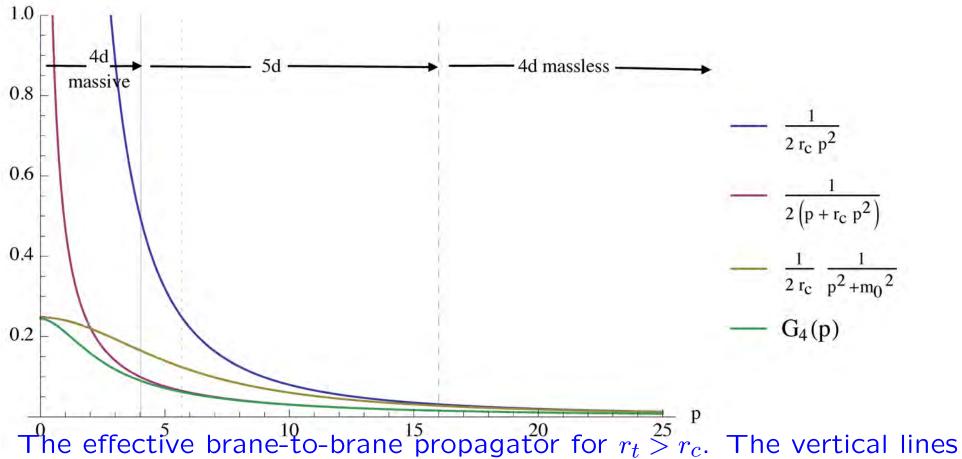
Massive gravity on the brane

• When $r_t > r_c$ we have three regimes for the gravitational interaction on the brane:

$$\tilde{G}_{4}(p) \simeq \begin{cases}
-\frac{e^{A_{0}}}{2r_{c}M^{d-1}} & \frac{1}{p^{2}} & p \gg \frac{1}{r_{c}} \\
-\frac{e^{A_{0}}}{M^{d-1}} & \frac{1}{2p} & \frac{1}{r_{c}} \gg p \gg m_{0} \\
-\frac{e^{A_{0}}}{2r_{c}M^{d-1}} & \frac{1}{p^{2} + m_{0}^{2}} & p \ll m_{0}, \quad m_{0}^{2} \equiv \frac{1}{2r_{c}d_{0}}
\end{cases}$$

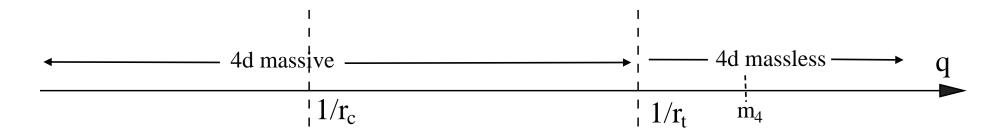
The 4d gravitational coupling is the same in both IR and UV regimes.

$$m_4^2 = e^{-2A_0} \frac{(d_0 d_2 - e^{-A_0} d_0^3 U_0)}{(d_2^2 2 - d_0 d_4)}$$



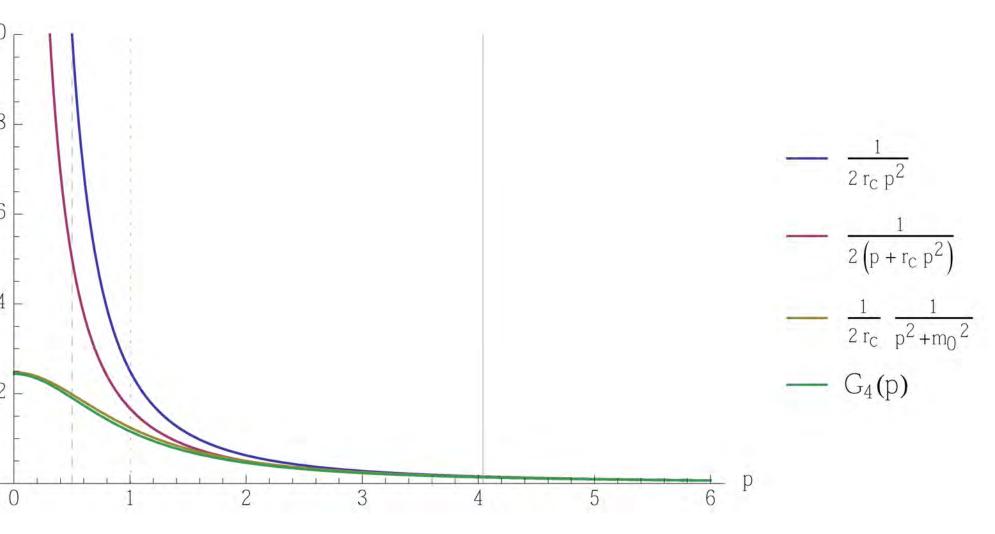
The effective brane-to-brane propagator for $r_t \stackrel{>}{>} r_c$. The vertical lines are: $1/r_t$ (solid), $1/r_c$ (dashed), m_0 (dotted).

- Massive 4d gravity $(r_t < r_c)$
- ullet In this case, at all momenta above the transition scale, $p\gg 1/r_t>1/r_c$, we are in the 4-dimensional regime of the DGP-like propagator.



- ullet Below the transition, $p\ll 1/r_t$, we have again a massive-graviton propagator.
- The behavior is four-dimensional at all scales, and it interpolates between massless and massive four-dimensional gravity.

Kiritsis+Tetradis+Tomaras



The effective brane-to-brane propagator for $r_t < r_c$. The vertical lines are: $1/r_t$ (solid), $1/r_c$ (dashed), m_0 (dotted).

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Scalar Perturbations

- The next step is to study the scalar perturbations. They are of interest as they might destroy the equivalence principle.
- The equations for the scalar perturbations can be derived and they are complicated.
- Unlike previous analysis of similar systems they cannot be factorized to a relatively simple system as the graviton.
- There are two scalar modes on the brane:
- In one gauge, the brane bedding mode can be "eliminated" but the scalar perturbation is discontinuous on the brane.
- In another gauge the perturbation is continuous but the brane bending mode is present.

The effective quadratic interactions for the scalar modes are of the form

$$S_4 = -\frac{\mathcal{N}}{2} \int d^4x \sqrt{\gamma} ((\partial \phi)^2 + m^2 \phi^2)$$

• We need both $\mathcal{N} > 0$ and $m^2 > 0$.

The conditions that the scalars are not ghosts are

$$\tau_0 \equiv 6 \frac{W_B}{W_{UV} W_{IR}} \Big|_{\Phi_0} - U_B(\Phi_0) > 0 \quad , \quad Z_0 \tau_0 > 6 \left(\frac{dU_B}{d\Phi} \right)^2 \Big|_{\Phi_0} \tag{1}$$

Asking also for no tachyons we obtain

$$\left. \frac{d^2 W_B}{d\Phi^2} \right|_{\Phi_0} - \left[\frac{d^2 W}{d\Phi^2} \right]_{UV}^{IR} > 0$$

- In general the two scalar modes couple to two charges: the "scalar charge" and the trace of the brane stress tensor.
- The mode that couples to the scalar charge has a "heavy" mass of the order of the cutoff.
- The mode that couples to the trace of the stress-tensor has a mass that is O(1) in cutoff units (like the graviton mass).
- All the stability conditions for the scalars depend on more details of the brane induced functions $W_B(\Phi)$, $U_B(\Phi)$, $Z_B(\Phi)$.
- They can be investigated further from the known parameter dependence of the vacuum energy.

 Kounnas+Pavel+Zwirner, Dimopoulos+Giudince+Tetradis
- There is a vDVZ discontinuity that (as usual) cannot be cancelled at the linearized order if the theory is positive.
- It should be cancelled by the Vainstein mechanism. To derive the relevant constraints on parameters, we must study non-linear solutions of sources on the brane.

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Detailed plan of the presentation

- Title page 0 minutes
- Bibliography 1 minutes
- Introduction 2 minutes
- Higher dimensions 3 minutes
- Brane worlds and early attempts 5 minutes
- Emerged Holographic gravity and the SM 7 minutes
- 1rst order RG flows 13 minutes
- Brane and bulk equations 20 minutes
- Old Self-Tuning 21 minutes
- Self-Tuning 2.0 23 minutes
- Linear Perturbations around a flat brane 26 minutes
- Induced Gravity 28 minutes
- The gravitational interaction on the brane 35 minutes

- The characteristic scales 39 minutes
- Massive gravity on the brane 41 minutes
- More on scales 42 minutes
- Scalar Perturbations 44 minutes
- dS or AdS solutions on the brane 46 minutes
- Cosmology 52 minutes
- Connecting the Hierarchy Problem 54 minutes
- Holographic axions 56 minutes
- Conclusions and Outlook 57 minutes

- A simple numerical example 59 minutes
- The bulk propagator 63 minutes
- Scalar Perturbations 65 minutes
- RG 68 minutes
- Detour: the local RG group 71 minutes
- Massive gravity on the brane 75 minutes
- Scalar Perturbations 79 minutes

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